

Revised Effective Ionic Radii and Systematic Studies of Interatomic Distances in Halides and Chalcogenides

BY R. D. SHANNON

Central Research and Development Department, Experimental Station, E. I. Du Pont de Nemours and Company, Wilmington, Delaware 19898, U.S.A.

(Received 30 October 1975; accepted 9 March 1976)

The effective ionic radii of Shannon & Prewitt [*Acta Cryst.* (1969), B25, 925–945] are revised to include more unusual oxidation states and coordinations. Revisions are based on new structural data, empirical bond strength–bond length relationships, and plots of (1) radii *vs* volume, (2) radii *vs* coordination number, and (3) radii *vs* oxidation state. Factors which affect radii additivity are polyhedral distortion, partial occupancy of cation sites, covalence, and metallic character. Mean Nb⁵⁺–O and Mo⁶⁺–O octahedral distances are linearly dependent on distortion. A decrease in cation occupancy increases mean Li⁺–O, Na⁺–O, and Ag⁺–O distances in a predictable manner. Covalence strongly shortens Fe²⁺–X, Co²⁺–X, Ni²⁺–X, Mn²⁺–X, Cu⁺–X, Ag⁺–X, and M–H[–] bonds as the electronegativity of X or M decreases. Smaller effects are seen for Zn²⁺–X, Cd²⁺–X, In³⁺–X, Pb²⁺–X, and Tl⁺–X. Bonds with delocalized electrons and therefore metallic character, *e.g.* Sm–S, V–S, and Re–O, are significantly shorter than similar bonds with localized electrons.

Introduction

A thorough and systematic knowledge of the relative sizes of ions in halides and chalcogenides is rapidly being developed by crystal chemists as a result of (1) extensive synthesis within certain structure types, *e.g.* rocksalt, spinel, perovskite and pyrochlore; (2) preparation of new compounds with unusual oxidation states and coordination numbers; and (3) the abundance of accurate crystal structure refinements of halides, chalcogenides, and molecular inorganic compounds. A set of effective ionic radii which showed a number of systematic trends with valence, electronic spin state, and coordination was recently developed (Shannon & Prewitt, 1969, hereafter referred to as SP 69). This work has since been supplemented and improved by studies of certain groups of ions: rare earth and actinide ions (Peterson & Cunningham, 1967, 1968); tetrahedral oxyanions (Kálmán, 1971); tetravalent ions in perovskites (Fukunaga & Fujita, 1973); rare earth ions (Greis & Petzel, 1974); and tetravalent cations (Knop & Carlow, 1974).

Further, the relative sizes of certain ions or ion pairs were studied by Khan & Baur (1972): NH₄⁺; Ribbe & Gibbs (1971): OH[–]; Wolfe & Newnham (1969): Bi³⁺–La³⁺; McCarthy (1971): Eu²⁺–Sr²⁺; Silva, McDowell, Keller & Tarrant (1974): No²⁺. These authors' results have been incorporated here into a comprehensive modification of the Shannon–Prewitt radii.

In this paper the revised list of effective ionic radii, along with the relations between radii, coordination number, and valence is presented. The factors responsible for the deviation of radii sums from additivity such as polyhedral distortion, partial occupancy of cation sites, covalence, and metallic behavior (electron delocalization) will be discussed.

Procedure

The same basic methods used in SP 69 were employed in preparing the revised list of effective ionic radii (Table 1). Some of the same assumptions were made:

(1) Additivity of both cation and anion radii to reproduce interatomic distances is valid if one considers coordination number (CN), electronic spin, covalency, repulsive forces, and polyhedral distortion.*

(2) With these limitations, radii are independent of structure type.

(3) Both cation and anion radii vary with coordination number.

(4) With a constant anion, unit-cell volumes of isostructural series are proportional (but not necessarily linearly) to the cation volumes.

Other assumptions made in SP 69 have been modified:

(1) The effects of covalency on the shortening of M–F and M–O bonds are *not* comparable.

(2) Average interatomic distances in similar polyhedra in one structure are *not* constant but vary in a predictable way with the degree of polyhedral distortion (and anion CN). Both of these modified assumptions will be discussed in detail later.

The anion radii used in SP 69 were subtracted from available average distances. Approximately 900 distances from oxide and fluoride structures were used, and Table 2 lists their references according to CN and spin. These references generally cover from 1969 to 1975. The cation radii were derived to a first approximation from these distances, and then adjusted to be consistent with both the experimental interatomic distances and radii–unit cell volume (*r*³ *vs* *V*) plots, as in

* Polyhedral distortion was not considered in SP 69.

Table 1 (cont.)

ION	EC	CN	SP	CR	'IR'	ION	EC	CN	SP	CR	'IR'	ION	EC	CN	SP	CR	'IR'
Na+1 2P 6 IV					.99	PR+3 4F 2 VI				1.13	.99 R	TC+4 4D 3 VI				.785	.645 RM
V					1.14	VIII				1.266	1.126 R	TC+5 4D 2 VI				.74	.60 ER
VII					1.16	IX				1.319	1.179 R	TC+7 4P 6 IV				.51	.37
VIII					1.26	PR+4 4F 1 VI				.99	.85 R	TE-2 5P 6 VI				2.07	2.21 P
VIII					1.32	VIII				1.10	.96 R	TE+4 5S 2 III				.66	.52
IX					1.38	PT+2 5D 8 IVSQ				.74	.60	IV				.80	.66
XII					1.53	IX				.94	.80 A	VI				1.11	.97
NB+3 4D 2 VI					.86	PT+5 5D 5 VI				.71	.57 ER	TE+6 4D10 IV				.57	.43 C
NB+4 4D 1 VI					.82	PU+3 5F 5 VI				1.14	1.00 R	VI				.70	.56 *
VIII					.93	PU+4 5F 4 VI				1.00	.86 R	TH+4 6P 6 VI				1.08	.96 C
NB+5 4P 6 VI					.62	VIII				1.10	.96	VIII				1.19	1.05 RC
VI					.78	PU+5 5F 3 VI				.88	.74 E	IX				1.23	1.09 *
VII					.83	PU+6 5F 2 VI				.85	.71 R	X				1.27	1.13 E
VIII					.88	RA+2 6P 6 VIII				1.62	1.48 R	XI				1.32	1.18 C
ND+2 4F 4 VIII					1.43	XII				1.84	1.70 R	XII				1.35	1.21 C
IX					1.49	RB+1 4P 6 VI				1.66	1.52	TI+2 3D 2 VI				1.00	.86 E
ND+3 4F 3 VI					1.123	VII				1.70	1.56 E	TI+3 3D 1 VI				.810	.670 RM
VIII					1.249	VIII				1.75	1.61	TI+4 3P 6 IV				.56	.42 C
VIII					1.303	VIII				1.77	1.63 E	V				.65	.51 C
XII					1.41	IX				1.80	1.66	VI				.745	.605 RM
NI+2 3D 8 IV					.69	X				1.83	1.69	VIII				.88	.76 C
IVSQ					.63	XI				1.86	1.72	TL+1 6S 2 VI				1.64	1.50 R
V					.77	XII				1.97	1.83	VIII				1.73	1.59 R
VI					.830	XIV				.77	.63 RM	XII				1.84	1.70 RE
NI+3 3D 7 VI	LS				.70	RE+4 5D 3 VI				.72	.58 E	TL+3 5D10 IV				.89	.75 R
LS					.74	RE+5 5D 2 VI				.69	.55 E	VI				1.025	.885 R
NI+4 3D 6 VI	LS				.62	RE+6 5D 1 VI				.52	.38	VIII				1.12	.98 C
ND+2 5F14 VI					1.24	RE+7 5P 6 IV				.67	.53	TM+2 4F13 VIII				1.17	1.03 R
NP+2 5F 5 VI					1.24	RH+3 4D 6 VI				.85	.65 R	TM+3 4F12 VI				1.23	1.09
NP+3 5F 4 VI					1.15	RH+4 4D 5 VI				.74	.60 RM	VIII				1.020	.880 R
NP+4 5F 3 VI					1.12	RH+5 4D 4 VI				.69	.55	VIII				1.134	.994 R
VIII					1.12	RH+6 4D 3 VI				.62	.48	IX				1.192	1.05 R
NP+5 5F 2 VI					.89	RH+7 4D 2 VI				.55	.41	U +3 5F 3 VI				1.165	1.025 R
NP+6 5F 1 VI					.86	RU+8 4P 6 VI				.760	.620 RM	U +4 5F 2 VI				1.03	.89
NP+7 6P 6 VI					.85	RU+5 4D 3 VI				.705	.565 ER	VIII				1.09	.95 E
O -2 2P 6 II					1.21	RU+7 4D 1 VI				.52	.38	IX				1.14	1.00 RM
II					1.22	RU+8 4P 6 VI				1.36	1.20	IX				1.19	1.05
IV					1.24	S -2 3P 6 VI				1.70	1.84 P	XII				1.31	1.17 E
VI					1.26	S +4 3S 2 VI				.51	.37 A	U +5 5F 1 VI				.90	.76
VIII					1.28	S +6 2P 6 IV				.26	.12 *	VI				.98	.86 E
OH-1					1.18	SB+3 5S 2 VPVY				.63	.29 C	IV				.98	.86 E
III					1.20	V				.90	.76	IV				.66	.52
IV					1.21	V				.94	.80	VIII				.87	.73 *
VI					1.23	SB+5 4D10 VI				.90	.76 A	VIII				.95	.81 E
HS					.74	SC+3 3P 6 VI				.885	.745 RM	VIII				1.00	.86
OS+4 5D 4 VI					.770	SE-2 4P 6 VI				1.010	.870 RM	V +2 3D 3 VI				.93	.79
OS+5 5D 3 VI					.715	SE+4 4S 2 VI				1.84	1.93 P	V +3 3D 2 VI				.780	.640 RM
OS+6 5D 2 V					.63	SE+6 3D10 IV				.42	.28 *	V +4 3D 1 V				.67	.53
OS+7 5D 1 VI					.685	SE+8 2P 6 IV				.56	.42 C	VI				.72	.58 RM
OS+8 5P 6 IV					.53	SI+4 2P 6 VI				.60	.42 *	VIII				.86	.72 E
P +3 3S 2 VI					.58	V				.940	.400 RM	V +5 3P 6 IV				.60	.46 *
P +5 2P 6 IV					.31	SM+2 4F 6 VIII				1.36	1.22	V				.60	.46 *
V					.43	VIII				1.41	1.27	W +4 5D 2 VI				.68	.66 RM
VI					.52	IX				1.46	1.32	W +5 5D 1 VI				.76	.62 *
PA+3 5F 2 VI					1.18	SM+3 4F 5 VI				1.098	.958 R	W +6 5P 6 IV				.56	.42 *
PA+4 6D 1 VI					1.04	VII				1.16	1.02 E	V				.65	.51
VIII					1.15	VIII				1.219	1.079 R	VI				.74	.60 *
VIII					.92	IX				1.272	1.132 R	XE+8 4D10 IV				.54	.40
VIII					1.05	XI				1.38	1.24 C	VI				.62	.48
IX					1.09	XII				.69	.55 R	Y +3 4P 6 VI				1.040	.900 RM
PB+2 6S 2 VPVY					1.12	SN+4 4D10 IV				.76	.62 C	VIII				1.159	1.019 R*
VI					1.33	V				.830	.690 RM	IX				1.215	1.075 R
VIII					1.37	V				.89	.75	YB+2 4F14 VI				1.16	1.02
VIII					1.43	SR+2 4P 6 VIII				1.32	1.18	VIII				1.22	1.08 E
IX					1.49	VIII				1.35	1.21	VIII				1.28	1.14
X					1.54	IX				1.40	1.26	YB+3 4F13 VI				1.008	.868 RM
XI					1.59	IX				1.45	1.31	VI				1.065	.925 E
XII					1.63	X				1.50	1.36 C	VIII				1.125	.985 R
V					.79	XII				1.58	1.44 C	IX				1.182	1.042 R
V					.87	TA+3 5D 2 VI				.86	.72 E	ZN+2 3D10 IV				.74	.60 *
VIII					.915	TA+4 5D 1 VI				.82	.68 E	V				.82	.68 *
VIII					1.08	TA+5 5P 6 VI				.78	.64 *	VI				.880	.740 RM
IX					1.08	VIII				.83	.69	VIII				1.04	.90 C
PD+1 4D 9 II					.73	.88				.74	.58	ZR+4 4P 6 IV				.73	.59 R
PD+2 4D 8 IVSQ					.78	TB+3 4F 8 VI				1.063	.923 R	V				.80	.66 C
PD+3 4D 7 VI					1.00	V				1.12	1.00 E	VI				.86	.72 RM
PD+4 4D 6 VI					.755	VIII				1.180	1.040 R	VIII				.92	.78 *
PD+5 4D 5 VI					1.11	IX				1.235	1.095 R	VIII				.98	.84 *
PD+6 4D 4 VI					1.23	IX				.90	.76 R	IX				1.03	.89
PD+7 4D 3 VI					1.284	IX				1.02	.88						
PD+8 4D 2 VI					1.08	TB+4 4F 7 VI											
PD+9 4D 1 VI					1.22	VIII											
PD+6 5D10 VI					.81												

VIII V^{4+} , IV Pb^{4+} , and X Th^{4+} obtained from these plots were used to help determine the values in Table 1. The first estimate of VIII V^{4+} was made from distances in $\text{C}_{32}\text{H}_{28}\text{S}_8\text{V}$ (Bonamico, Dessy, Fares & Scaramuzza, 1974).

Another method used to estimate radii was based on the empirical relationship between interatomic distances and bond strengths. Brown & Shannon (1973) derived these relationships for the cations in the first three rows of the periodic table from a large number of experimental interatomic distances. These curves can be used to calculate hypothetical distances for cations in any coordination (Brown & Shannon, 1973; Shannon, 1975; Brown, 1975). Examples of cations whose radii were calculated in this way are: IV Mn^{2+} , VI Be^{2+} , VI B^{3+} , VI P^{5+} , VI S^{6+} , VIII Mg^{2+} , and VIII Fe^{2+} . These are marked with a C in Table 1. In certain cases, these values were combined with known structural data (see Table 2) to obtain the radii in Table 1. Although the

majority of radii were derived from oxides and fluorides,* some were taken from chlorides, bromides, iodides, and sulfides. For large electropositive cations with highly ionic bonds, very little covalent shortening is believed to occur and radii derived from these other compounds should differ only slightly from those derived from fluorides and oxides. Examples are divalent rare earths such as Yb^{2+} , Tm^{2+} , Dy^{2+} , Sm^{2+} , Nd^{2+} and the ions Am^{2+} , Ac^{3+} , Np^{3+} , and U^{4+} .

Another useful scheme for estimation of radii is the comparison of unit-cell volumes of compounds containing cations of similar size. McCarthy (1971) prepared a number of isotopic Sr^{2+} and Eu^{2+} ternary oxides and generally found the unit cells of the Sr^{2+}

* Because of covalency differences in M-O and M-F bonds, oxide distances were emphasized. Therefore the radii in Table 1 are more applicable to oxides than fluorides. This subject is treated further in the discussion *Effects of covalence*.

Table 2. References for Table 1

The references here and in Tables 4, 5, 6 and 8 are abbreviated according to *Codens for Periodic Titles* (1966).

AC*3 VI
68 JINCA 30 823 AC CL3
AG*1 I1
71 INOCA 10 719 AG FE 02
72 ZAACA 393 246 SA AG 04
73 ZENBA 288 263 BA AG 04
AG*1 IV
71 JSSCB 3 364 AG 02 CR 04
42 JACSA 64 354 AG 03 AS 04
69 ACSAA 23 2261 AG 2 S 03
AG*1 V
70 JSSCB 1 484 AG 06 MO10 033
32 ZKXKA 82 161 AG 02 S04
47 JACSA 69 222 AG 03 PD
71 JSSCB 3 364 AG 02 CR 04
69 ACAB 25 5116 AG 02 CR 07
70 JSSCB 1 484 AG 02 MO 04
AG*1 VII
70 JSSCB 1 484 AG 06 MO10 033
59 ACAB 25 5116 AG 02 CR 07
AG*1 VIII
65 ACCRA 19 180 AG 7 M 011
AG*2 IVS0
71 JPSCA 32 543 AG F2
AG*2 VI
71 JPSCA 32 543 AG F2
AG*3 IVS0
65 ACCRA 19 180 AG 7 M 011
AL*3 V
67 ACRA 23 754 NA 112 AL 05 012
68 NJMHA 1968 80 CA AL B 04
70 AGBA 26 1230 CA AL A 01
71 SPMDA 1970 547 CALT AL 03
71 SPMDA 15 905 CA AL 010 (OM)16
71 SPMDA 15 905 CA AL 010 (OM)16
71 AGBA 27 1820 BETA-AL2 03
72 JSSCB 4 60 AG AL11 017
AL*3 V
68 ACBA 24 1518 (MG+FE) AL 51 B 09
68 AMMIA 53 1096 AL 2 PD4 10H13
AL*3 VI
71 AMMIA 56 18 NA3 AL 2 L13 F12
72 JSSCB 4 11 NO AL 03
72 JSSCB 4 11 NO AL 03
58 ACCRA 5 684 MG AL 2 04
72 ACBA 28 1899 AL 2 BE3 S10 D18
68 JACSA 89 2201 AL 1 CA 03
73 ACBA 28 1899 AL 2 BE3 S10 D18
67 ZKXKA 125 1423 CS BE4 B112-X1 AL4 O28 H2
74 ACBA 30 1312 NA AL 04 D12 IO H14
74 ZKXKA 130 125 AL IO H13
AM*2 VII
72 JINCA 34 3427 AM 12
AM*2 VIII
73 JINCA 35 483 AM BR2
AM*2 IX
73 JINCA 35 483 AM CL2
AM*3 VIII
11 2233 AM 2 (S O4)3 BH2 0
AM*4 VI
67 ADCSA 71 228 BA AM 03
67 INUCA 3 327 R (BK+)
AS*5 IV
69 ZKXKA 130 231 2M 02 AS 02 08
68 CJCHA 46 917 CU 3 AS 02 08
63 BAPCA 11 361 MG 02 AS 07
69 ACBA 25 1544 CA M AS 04.2 H2 0
69 ACBA 25 2658 ZR 1M AS 04.12 H2 0
68 AMMIA 53 1841 M2 0 M AS 04
63 CARMA 7 561 CA CU AS 04 0 M
70 ACBA 26 1824 NA 2 AS 04.7 H2 0
70 ACBA 26 1574 NA 2 H AS 04.7 H2 0
69 CHDCA 268 1694 BA H12 AS 02 08
70 AMMIA 55 2023 M99 IO H19 (H2 O)2
(AS O3) (AS O4)2
70 ACBA 26 1889 1M H012 H AS 04
24 3711 LI 1 MO 02 AS 04
70 INOCA 9 2259 CA 2 AS 04 CL
65 ACCRA 18 777 CU 3 AS 04 IO H13
70 CJCHA 48 890 MG 02 AS 02 08
70 CJCHA 48 891 CU 3 AS 02 08
71 CJCHA 49 1036 AL 3 AS 02 08
70 AMMIA 55 1489 M7 S 05 O12
71 ACBA 27 2124 NA 3 AS 04.12 H2 0
73 ACBA 29 2811 MG 02 AS 08
61 AMMIA 46 1077 CA 2 B AS 04 (OM)4
73 CJCHA 51 2082 NA 4 AS 02 07
66 ZACBA 347 1314 H AS 04 H2 0
66 ZACBA 347 140 SR H AS 04 H2 0
71 AMMIA 56 1147 2NA AS 02 (OM)2.2H2 0
70 ACBA 26 403 CA H AS 04
70 ZKXKA 132 332 CU 3 AS 02 08
73 ACBA 29 141 LU AS 04
73 ACBA 29 2121 MM 02 AS 04
AS*5 VI
71 CJCHA 49 2539 CL F2 AS 04
73 JSSCB 6 80 MGB 5 AS 03 016
70 CJCHA 48 3124 CD 8 AS 03 016
73 ACAD 29 286 CALCULATED
74 INOCA 13 780 XL AS F11.4E2 AS F9
74 ACBA 30 250 R AS F6
AU*3 IVS0
67 JCSIA 1969 1936 R AU F4
70 ZACBA 375 243 L13 AU O3.4 AU O2.8B AU O2
70 JCSIA 1970 1092 R AU (OM)31
AU*3 V
74 INUCA 13 775 RE 2 AU F17
D *3 III
68 NJMHA 1968 80 CA AL B 04
70 ACBA 28 906 B 03 1
71 SPHCA 15 802 K BE 2 B 03 F2
71 ACBA 27 872 2M B 04 07
70 ACBA 26 1189 R B 02
71 ACBA 27 904 L13 B 03
70 ZKXKA 132 241 CA B 3 05 (OM)1
71 JACCA 4 284 CU B 4
74 JPSCA 60 1899 MM B 4 07
74 MRBUA 9 1661 ND AL 1 (B 03)14
B *3 IV
68 ACBA 24 869 B 2 J 11
66 ACBA 24 1703 NA B F4
68 CJCHA 47 877 R B F4
71 ACBA 47 877 CU B 2 04
71 ACBA 132 241 CA B 3 05 O H
63 ACCRA 16 1233 NA B U H1+2 H2 0
74 JINCA 60 1899 MM B 4 07
71 AMMIA 56 1553 MG (NO 07 IO H16) 1.2 H2 0
71 AMMIA 58 909 CA B 51 U4 0 H
71 ACBA 27 872 2M B 04 07
B *3 V
72 ACAB 29 286 CALCULATED
BA*2 VI
70 ZKXKA 131 161 BA 3 V 08
73 ZENBA 288 263 BA AG 04
BA*2 VII
71 ACBA 47 1263 BA FE 04
73 ACBA 29 2009 BA 2 T1 04
BA*2 VIII
58 ZKXKA 110 231 CU B 2 IC U D H16.4 H2 0
69 JCPSCA 51 4928 BA MM F4
70 JPSCA 53 3279 BA CU F4

71 JCPSCA 55 1093 BA W 04
71 AMMIA 56 758 BA C 03
71 ZACBA 386 1 BA 2 CO 04
73 ACBA 29 2009 BA 2 T1 04
BA*2 IX
71 ZACBA 386 1 BA 2 CO 04
73 ACBA 27 1695 BA TE 152 O312.2 H2 0
73 ACSAA 27 1653 BA TE 152 O312.3 H2 0
BA*2 X
70 ZKXKA 131 161 BA 3 IV 0412
70 ACBA 26 105 BA 3 S14 NB6 D26
67 BFCBA 90 24 BA P2 06
BA*2 XI
71 ACBA 27 1263 BA FE 04
BA*2 XII
70 ACBA 26 102 BA 5 TA 015
72 CSCMC 1 1 BA T16 013
71 MRBUA 6 725 BA CA FE 08
69 CHDCA 288C 1694 BA H12 H2 08
75 ACBA 31 596 K2 BA CU (N D2)16
BE*2 I
69 ACBA 25 1647 SR BE 3 04
66 ACBA 20 295 CA12 BE17 O29
BE*2 IV
62 SPHCA 6 733 NA BE P 04
68 ACBA 24 672 LA 2 BE 05
68 ACBA 24 607 CS BE F 3
69 ACBA 25 1847 SR BE 3 04
71 SPHCA 15 999 FE 3 BE S13 09 (F,DH)2
72 SPHCA 16 1021 BE 2 S1 04
72 ACBA 28 1899 AL 2 BE 516 D18
73 ACBA 229 2976 NA 3 BE TH10 F45
69 ACBA 12 434 BE FATE
67 ZKXKA 125 423 CS BE4 B112-X1 AL4 O28 H2
74 ACBA 30 396 NA6 (S116 AL2)(HE(DH)2 O39)
L15 H2 0
74 ACBA 30 2434 L12 BE S1 04
74 AMMIA 59 1267 CA BE 2 P 08
BI*3 V
69 JSCOA 7 1797 B12 M 06
70 ACSAA 24 384 B12 O3 ALPHA
BI*3 VI
70 ACSAA 24 384 B12 O3 ALPHA
71 JPSCA 32 1315 B1 FE 03
BI*3 VII
72 MRBUA 7 1025 B1 TITANATES
BI*3 VI
R3 VS V (BA2 LA B1 O6)
BR*4 VI
67 INUCA 3 327 R (BK+)
BR*4 IV S0
69 JCSIA 1969 1936 K BA F4
BR*5 I11
69 ACBA 25 421 SR (BR O3)3.9H2 0
67 ACSAA 21 2834 MG BR 03
BR*7 IV
71 JCSIA 1971 1857 BR(+7)0
C*4 I11
65 ACCRA 18 689 CA C 03
71 JHEAR 754 27 CA C 03
73 AMMIA 58 1029 MG C 03
67 PLAA 92 125 MM C 03
75 ACBA 31 890 NA 2 C O3.H2 0
CA*2 VI
68 NJMHA 1968 80 CA AL B 04
69 ACBA 25 1933 CA AL 1M2 P O213
57 JPCSA 26 563 CA IO H12
55 ACCRA 18 689 CA C 03
CA*2 VII
71 CJCHA 49 1036 CA 3 AS 02 08
71 ACBA 27 2311 CA 2 AL FE 05
73 MRBUA 8 593 CA CR F 5
69 ACBA 25 1534 CA10 (P O4)16 IO H12
CA*2 VIII
71 INOCA 7 1345 CA 2 P 02
74 CJCHA 52 1155 CA18 MG 2 H (P O4)14
CA*2 IX
71 JHEAR 754 27 CA C 03
69 ACBA 25 1534 CA10 (P O4)16 IO H12
CA*2 X
69 ACBA 25 955 CA B 2 O4 111
CA*2 XI
69 ACBA 25 965 CA B 2 O4 1V
74 AMMIA 59 41 CA AL 3 IO H16
74 JACSA 96 6606 K2 CA CU IN D216
CO*2 IV
59 ACCRA 12 1049 CO 1 H2 04
71 ZACBA 382 270 K CO 02 03
CO*2 V
69 CJCHA 47 3409 CO 2 P 02
70 ZKXKA 132 332 CU 3 AS 02 08
CO*2 VI
69 CJCHA 47 3409 CO 2 P 02
70 ZKXKA 132 332 CU 3 AS 02 08
60 SPHCA 11 11 CO M 04
67 HCAGA 50 2023 CO HNS 08
74 JCSIA 1974 676 CO CA H6 06
74 ACBA 30 1880 CO 2 CA H12 012
CO*2 VII
74 ACSAA 28A 119 CO D1C H 2 C O D12.3 1/2 H2 0
74 JCSIA 1974 1922 CO O3 H5 05
CO*2 VIII
55 PRVBA 98 903 CO 2 H2 07
69 ACBA 25 1806 CO IN O312.4 O2 U
74 JCSIA 1974 676 CO CA H6 06
CE*3 VIII
74 ZACBA 403 1 R3 VS V (CE F3)
74 JCSIA 1974 1165 CA1 H24 CE F12 M 08 54
CE*3 IX
67 SPHCA 12 214 CE B S1 05
74 ZACBA 403 1 R3 VS V (CE F3)
CE*3 X
60 AMMIA 45 1 CE4 ME H2 T2 S14 D22
CE*4 VI
72 ACBA 28 956 BA CE 03
73 JSSCB 8 331 R (CE+)
CE*4 VIII
69 INUCA 8 33 (N H6)2 CE F6
74 JCSIA 1974 2021 NA6 CE M10 D36.2H0.2H2 0
74 JCSIA 15 397 CE15 O12
74 ACSAA 28 1079 A CE 1ACAG14
CE*4 XII
68 JACSA 90 3589 (HMH)2 H6 ICE M012 O421.12 H2 0
CF*3 VI
74 JINCA 36 2023 R3 VS V (CF 2 S O4)3
CL*7 IV
73 MRBUA 8 791 RB CL 03
CL*7 V
72 ACBA 28 839 TMPO CL 04
72 ZKXKA 84 65 K CL 04
60 ACBA 13 855 M UZ CL O4 H CL O4
H CL O4 H2 O4 L CL O4.3 H2 0
59 JPCHA 63 279 H CL O4 H2 0
98 JACSA 80 5075 CE H6 H CL O4
57 PISSA 96 136 H H CL O4
57 PISSA 96 143 R CL O4
62 ACBA 15 1201 W H CL O4
71 JCSIA 1971 1371 CU (ClO H9 N312 ICL O4)2
70 ACBA 26 1928 H5 CL O4
71 ACBA 27 898 H CL O4 1/2 H2 0
73 ICHAA 7 477 IC N12-TALEN-CL O4
71 ACBA 27 898 H CL O4 2 1/2 H2 0

72 MRBUA 7 1281 CL1(+7)0
71 JCSIA 1971 1857 CL1(+7)0
62 ACCRA 15 18 H3 O CL O4 (180 C1
69 ACBA 25 1875 H3 O CL O4
73 ACSAA 27 2309 (P84 IO H14)3 C O3 (CL O4)10
66 H2 0
73 ACSAA 27 3523 CU (C3 H6 N214 ICL O4)2
LM*4 VI
67 INUCA 3 327 R (CE+)
CO*2 IV
69 ZACBA 369 306 CO V2 04
CO*2 V
72 ACBA 28 2883 CO 2 P 02 ALPHA
CO*2 VI
68 ZACBA 358 125 CO SE 04
68 ZKXKA 126 298 CO SE 03
70 CJCHA 48 881 CO 3 AS 02 08
70 JPCSA 53 3279 BA CO F4
70 PERIA 3 131 CO 2 S1 04
73 ACBA 29 2304 CO 3 V 08
71 HCAGA 54 1621 CO 3 IO H12 (S O4)2.2 H2 0
REF 1 CO 2 S1 04
72 ACBA 28 2883 CO 2 P 07
70 INOCA 9 151 CO (OM)13 (CL O4)2
73 ACBA 29 2741 CO S1 F4.6 H2 0
74 AMMIA 59 475 CO 2 S1 04
74 JCLMB 4 55 C16 H18 CO 06
CO*2 VIII
66 INUCA 5 1208 (AS16 H514)2(COIN O3)3
CO3 VI
68 CJCHA 1968 871 CO (N O3)3
68 CJCHA 46 3472 CO 3 04
66 JACSA 88 2951 CO (C5 M7 O2)13
74 ACBA 30 822 CO H2 O7 O23
69 JACSA 91 8881 IN H416 (H4 CO 2 MO10 O38)1
H2 0
74 ZACBA 408 97 K CO 2 04
CO*4 IV
71 ZACBA 386 1 BA 2 CO 04
73 ZACBA 398 54 L18 CO 06
74 ZACBA 408 75 CS 2 CO 03
74 ZACBA 409 152 K CO 2 07
CO*4 V HS
67 STGBA 3 1 R3 VS V (FLUORIDES)
74 ZACBA 408 97 K CO 2 04
CR*2 VI LS
71 ANCPA 6 41 TA 2 CR 06
69 ACBA 25 925 R VS O ELECTRONS
CR*4 VI
69 MRBUA 4 621 NA 3 CR F6
70 INOCA 9 2289 NA 3 (CR MO 06 O24 H6)1.8 H2 0
70 ACBA 24 3627 NA 2 CR 3 08
73 MRBUA 8 593 CA CR F 5
65 ACCRA 19 131 CR (C5 H7 O2)3
CR*4 IV
74 ZACBA 407 129 BA 2 CR 04
CR*4 V
72 MRBUA 7 157 CR 02
CR*5 VI
67 STGBA 3 1 R3 VS V (FLUORIDES)
CR*6 IV
68 CJCHA 46 935 K 2 CR 07
70 ACBA 26 222 CR 03
69 JCSIA 1969 1857 (H4)12 CR 04
69 ACBA 25 5116 AG 02 CR 07
70 SPMDA 15 530 K 2 CR 03
70 AMMIA 55 784 P 2 CR 05
70 ACSAA 24 3627 M2 CR 3 08 O H
71 SPHCA 15 820 NA 2 CR 02.2 H2 0
71 SPHCA 15 826 L12 CR 02.2 H2 0
73 ACBA 29 890 NA 2 CR 07 ALPHA
74 ACSAA 25 44 H3 2 CR 04
70 CJCHA 48 537 RB 2 CR 07
71 ACSAA 25 35 RB 2 CR 07
71 JSSCB 3 364 AG 02 CR 04
72 ACBA 28 2883 K 2 CR 04
73 ACSAA 27 177 2R6 IO H16 (CR O4)5.H2 0
73 ACBA 29 2181 RB 2 CR 03
73 ACBA 29 2963 NA 2 CR O4.4 H2 0
71 JCSIA 1971 1857 (H4)12 CR 04
73 MRBUA 8 271 2 CR 02 04
CR*6 VI
74 AMMIA 59 1160 P 86 CR CL 6 X6 Y2
CS*1 VIII
69 SPHCA 13 930 CS 2 BE F10
CS*1 IX
69 INOCA 8 1665 CS 5 MG F4
69 SPHCA 13 930 CS 2 BE F4
CS*1 X
69 INOCA 8 1665 CS 5 MG F10
CS*1 XI
67 ACBA 23 865 CS U F6
68 ACSAA 22 2793 CS CO CL 3
71 ACBA 27 245 CS U6 F25
CU*1 II
69 ZKXKA 129 259 CU LA O2
70 ZACBA 374 113 SR CU 2 O2
CU*1 IV
REF 2 CU F6 CU CL U BR
69 ACBA 2 158 K 2 CU CL 3
CU*1 VI
70 MRBUA 5 207 CU TA 03
CU*1 VII
57 ACCRA 10 556 CU CR 04
71 ACIEA 10 413 SR CU F4 CA CU F4
CU*2 IV S0
67 ZKXKA 124 91 2M 02 AS 02 08
68 ACBA 24 388 CU 2 H2 05
71 ACBA 27 877 CU B 2 04
65 JPCSA 43 3959 CU (C6 H5IC H3)2 C3 O212
66 INOCA 5 517 CU (ClO H9 O2)12
67 JCSIA 1967 309 CU (IO CL 2 H6)3
66 PLAA 289 161 CL4 H10 O4 CU
70 ACBA 26 8 CU 04
CU*2 V
69 ACSAA 23 221 CU 3 M 06
68 CJCHA 46 917 CU 2 08
68 JPCSA 48 2619 CU MO 04
CU*2 VI
63 NATUA 197 70 CU 3 S O4 0 H
63 ACCRA 16 124 CU 5 (P O4)2 IO H14
68 JPCSA 48 2619 CU MO 04
70 ACBA 26 1020 CU MO 04
68 CJCHA 46 805 CU 2 P 07
68 JACSA 90 5623 CU (IC H3)2 N12 -
(P O12) O13 (CL O4)2
CU*1 VII
70 INOCA 9 151 CU (OM)13 (CL O4)2
73 ACBA 29 1743 CU V2 06
CU*1 VIII
72 MRBUA 7 913 LA CU 03
DY*2 IV
UNPUI 0Y 12
DY*2 VIII
M CL O4 H2 O4 L CL O4.3 H2 0
UNPUI 0Y 12
DY*2 VIII
UNPUI 0Y CL2
DY*3 VI
63 PHSSA 3 8446 DY 2 03
DY*3 VII
15 1201 W H CL O4
DY*3 VIII
71 JCLMB 1 83 DY (TM)13.H2 0
DY*3 VIII
74 ZACBA 408 1 R3 VS V (DY F3)
70 SSCDA 8 1745 DY FES 012
DY*3 IX

Table 2 (cont.)

74 ZAACA 403 1 R3 VS V (DY F3)
ER+3 VI
70 ACBCA 26 484 ER2 S12 07
ER+3 VII
70 SPHCA 15 36 ER2 GEZ 07
72 JCMDB 2 197 ER8 U (THD)10 IO H112
ER+3 VIII
08 CHPLB 2 47 ER P 04; ER V 04
70 INOCA 9 2100 IC2 04; IM G2 04; JH2 0
70 SSCGA 8 1745 ER3 FE5 U12
71 ACSAA 25 172 ER IM U C H2 C D 013; 2H2 0
74 ZAACA 403 1 R3 VS V (ER F3)
72 JCMDB 2 197 ER8 U (THD)10 IO H112
ER+3 IX
59 ZKAKA 112 362 ER IC2 H5 S 0413; 9H2 0
74 ZAACA 403 1 R3 VS V (ER F3)
EU+2 VI
70 ZAACA 374 201 LI EU3 04
EU+2 VII
70 ZAACA 374 201 LI EU3 04
69 ACBCA 25 1104 EU 12 V (ER F3)
73 REF 3 L12 EU5 08
EU+2 VIII
UNPUI EU F2; EU BR2
73 RVGMA 10 77 EU CL2
UNPUI EU F2
EU+2 X
71 NATMA 58 218 EU2 S1 U4
EU+3 VI
08 REF 4 EU4 AL2 09
70 ZAACA 374 201 LI EU3 04
73 REF 3 L12 EU5 08
EU+3 VII
08 REF 4 EU4 AL2 09
73 REF 3 L12 EU5 08
EU+3 VIII
08 JCP5A 48 1094 EU3 FE2 GA3 012
74 ZAACA 403 1 R3 VS V (EU F3)
73 ACSAA 27 2827 EU2 (C3 H2 0413; 2H2 0
EU+3 IX
74 ZAACA 403 1 R3 VS V (EU F3)
73 ACSAA 27 2827 EU2 (C3 H2 0413; 2H2 0
71 ACSAA 25 3347 EU TRISULFOLATE
FE+2 IV SO HS
74 AMMIA 59 1166 BA FE S14 010
FE+2 IV HS
09 SCIEA 166 1399 IN4; K12 FE4 S112 030; H2 0
69 ZAACA 369 306 FE V2 04
71 JUP5A 31 452 FE2 T1 04
72 JUP5A 33 1296 FE T1 04
FE+2 VI LS
69 ACBCA 25 925 R VS A (FE S2)
FE+2 VI HS
69 NMMHA 1969 430 FE AL2 IP 0412 IO H12 IO H216
70 BUFGA 93 190 FE S 04
71 SPHCA 15 999 FE3 BE S13 09 (F; 0 H12
67 ACBCA 22 775 FE (IN4)1215 0412; 2H2 0
08 CMHTA 68 290 FE P 04
74 AMMIA 59 486 FE2 S1 04
FE+2 VIII
71 AMMIA 56 791 GARNETS
71 ZKRAA 134 333 FE3 AL2 S13 012
73 ACBCA 29 266 CALCULATED
FE+3 IV HS
70 ACBCA 26 1469 CA2 FE2 05
70 SSCGA 8 1745 ER3 FE5 U12
71 ACBCA 27 1263 BA FE2 04
71 MRBUA 6 725 BA CA FE4 08
71 ACSAA 25 3616 CA FE2 05
73 ACBCA 29 832 BA FE2 04
FE+3 V
71 JSSCB 4 1 FE V 04
FE+3 VI HS
70 ACBCA 26 1469 CA2 FE2 05
70 SSCGA 8 1745 ER3 FE5 U12
71 SSCGA 9 335 K FE F4
71 JSSCB 4 1 FE V 04
71 JCP5A 32 1315 FE 03
71 ACSAA 25 3616 CA FE2 05
69 ACBCA 23 239 FE IC5 HT 0213
69 CCJDA 1969 460 FE IC7 H5 0213
FE+3 VIII
71 JSSCB 8 331 ESTIMATED
FE+4 VI
73 JSSCB 8 331 R3 VS V (PEROVSKITES)
73 JSSCB 8 43 R2 FE 04
73 JSSCB 8 43 R3 VS V (K2 FE 04)
GA+3 IV
71 ACBCA 27 616 L15 04 04
75 ACBCA 31 568 SR GA S12 08
GA+3 VI
74 ACBCA 30 1364 C15 H21 06 GA
GD+3 VII
70 ACBCA 26 484 GD2 S12 07
72 ACBCA 28 60 GD2 M03 012
72 SPHCA 16 790 GD2 GE2 07
69 INVMA 5 1823 GD9; 33 S16 026
72 JSSCB 5 266 GD9; 33 S16 026
GD+3 VIII
71 SPHCA 15 926 NA GO S1 04
72 SPHCA 16 790 GD2 GE2 07
74 ZAACA 403 1 R3 VS V (GD F3)
GD+3 IX
72 SPHCA 16 790 GD2 GE2 07
69 INVMA 5 1823 GD9; 33 S16 026
74 ZAACA 403 1 R3 VS V (GD F3)
GE+4 IV
08 ZKAKA 126 299 CO GE 03
69 SCIEA 165 586 M2 GE 04
69 ZKAKA 129 427 M3 FE2 GE3 012
70 JSSCB 2 612 M228 GELIO 0+8
71 SPHCA 15 926 NA GO S1 04
70 ACSAA 24 1287 NA4 S2 GE4 012 IO H14
67 ACBCA 21 1281 NA8 S4 GE4 012 IO H14
70 MDCMB 102 964 NA2 GE 03
71 MDCMB 102 1245 R2 GE4 09
72 SPHCA 17 246 CO GE 03
72 MDCMB 103 1560 GE5 0 (P 0416
GE+4 VI
70 SSCGA 1 557 CA2 GE 04
70 JSSCB 2 612 M228 GELIO 0+8
71 MDCMB 102 1245 R2 GE4 09
71 ACBCA 27 2133 GE 02
72 AMMIA 57 62 M2 GE 04 DELTA
72 ZKAKA 136 387 GE IO H1 P 04
72 MDCMB 103 1560 GE5 0 (P 0416
H+1 I
57 JMD5A 1 43 T F
56 JCP5A 25 275 M F
H+4 IV
70 JSSCB 13 275 R3 VS V (M4 H 04)
H+4 VII
70 JACFA 53 126 HF 02
69 ACBCA 27 3341 HF IO H12 S 04; H2 0
74 ACFAA 27 3407 HF4 IOH18 IC4 0414; H2 0
H+4 VIII
73 ACSAA 27 2455 HF IO H12 S 04
H+4 VI
71 CCJDA 1971 468 M2 F2
H+4 II

73 ACBCA 29 869 HG MO 04
H+3 VIII
74 ACBCA 30 2049 K MO BE F6
70 SSCGA 8 1745 M03 FE5 U12
72 BUFGA 95 437 MO P5 014
74 ZAACA 403 1 R3 VS V (MO F3)
H+3 IX
74 ZAACA 403 1 R3 VS V (MO F3)
74 ACBCA 30 2613 M02C H5 S 0413; 2H2 0
H+4 I
74 INOCA 13 2535 M01H2 014 IM C 0313; 2H2 0
73 CJCHA 53 831 IN 012101M 03151
1+5 I
71 JCP5A 54 2556 N H4 I 03
66 ACBCA 20 758 LI 1 03
66 ZKRA 40 804 LI 1 03
58 ACCRA 9 1015 CE (1 0314
58 ACCRA 11 796 CE (1 0314; H2 0
43 TICFB 62 728 N H4 I 03
1+5 VI
71 JCP5A 54 2556 N H4 I 03
70 ACBCA 26 1782 NA I 04
28 ZEPFA 59 381 K I E 03
71 JCSIA 1971 1857 II+71 U
1+7 VI
71 ACCRA 20 765 H5 I U
65 ACCRA 19 629 K H2 I2 010; 2H2 0
37 JACSA 59 2036 IN H412 H3 I U
IN+3 IV
74 ZAACA 409 97 RB2 IN4 07
74 ZAACA 395 280 SR2 IN2 05
IN+3 VI
74 ZAACA 409 97 RB2 IN4 07
61 ACSAA 15 1437 IM D H S 04; 1H2 012
68 ACBCA 24 388 CUE IN2 05
70 ACSAA 24 1682 IN D 0 H
69 INOCA 8 1985 IN2 03
74 ACBCA 30 1982 M H4 FE S12 06
74 SPHDA 18 761 IN2 GE2 07
IR+4 VI
71 JSSCB 3 174 SR IR 03
71 ACBCA 98 266 K H2 (M3 03) 05 010
74 MRBUA 9 1177 R3 VS V (CO2 IR 02 07)
K+1 IV
68 ZAACA 358 241 K AG 0
REF 2
K+1 VI
51 ZAACA 264 144 K S8 F6
68 SPHDA 12 1095 K V M2 08
69 CCJDA 11 608 K2 H2 05
69 ACBCA 25 1919 K UZ F9
K+1 VII
68 CJCHA 46 935 K2 CR2 07
69 JCSIA 1969 849 K2 MO 04
71 SSCGA 9 345 K FE F4
K+1 VIII
70 ZKAKA 74 306 K H2 P 04
62 ZKRA 117 411 K2 T16 013
67 ZKRA 98 266 K H2 (M3 03) 05 010
71 INOCA 7 873 K H2 C 04
68 CJCHA 46 935 K2 CR2 07
70 JCSIA 1970 3092 K H2 IO 0314
65 ACCRA 19 629 K H2 I2 010; 2H2 0
K+1 IX
70 ZKAKA 132 27 K14 N4S5 CA0; 3 ALT-5
69 ACBCA 25 600 L15 F4 03
69 ACBCA 25 1919 K UZ F9
K+1 X
73 CJCHA 51 2613 K AL P2 07
K+1 XII
68 SPHCA 13 420 K V M2 08
71 INOCA 10 1264 K2 PB CU IN 0216
67 INOCA 5 514 K2 BA CO IN 0216
74 JACSA 96 6806 K2 CA CU IN 0216
75 ACBCA 11 594 K2 BA CU IN 0216
57 PISAIA 50 143 K CL 04
LA+3 VI
69 ZKAKA 129 259 CU LA 02
73 MRBUA 8 1269 R3 VS V (REZ M3 012)
LA+3 VIII
74 AMMIA 59 1277 LA6 M2 T13 S14 022
73 ACBCA 29 2074 LA6 M03 012
68 INOCA 7 2295 LA 65 HT 0213 (H2 012
74 ZAACA 403 1 R3 VS V (LA F3)
74 SPHCA 18 675 LA2 SR3 (B 0314)
LA+3 IX
71 MRBUA 6 23 LA FE 03
74 ZAACA 403 1 R3 VS V (LA F3)
74 AMMIA 59 1277 LA6 M2 T13 S14 022
L1+1 IV
39 ZKAKA 102 119 LI 0 H; H2 0
70 ZAACA 379 187 LI 02 07
70 INOCA 9 1096 YB LI F4
71 AMMIA 56 18 NA3 AL2 L13 F12
71 ACBCA 27 618 L15 04 04
73 JSSCB 6 538 L13 V 04
73 ACBCA 29 2625 LI IN2 H51 BE F4
73 ACBCA 29 2625 LI N H3 0 H S 04
64 ACBCA 17 793 L12 C2 04
74 ACBCA 30 2434 L12 BE S1 04
L1+1 VI
68 ACBCA 24 225 L13 AL F6
69 ZAACA 371 306 L12 IR 03
70 ZKRA 132 118 L12 AL2 S13 010
71 MRBUA 6 555 L12 MO F6
65 ACCRA 19 561 LI CO 07 H7
74 ACTEA 86 819 LI NB 02
68 CMHTA 68 290 LI FE P 04
71 ACSAA 25 3337 LI M03 08
73 CJCHA 51 265 LI V 03
73 ACBCA 29 2294 L12 ZA FE
LU+3 VI
70 ZAACA 377 70 CA LUZ 04
71 JACFA 4 284 LU B 03
LU+3 VIII
74 ZAACA 403 1 R3 VS V (LU F3)
LU+3 IX
74 ZAACA 403 1 R3 VS V (LU F3)
MG+2 IV
72 ACBCA 28 267 K2 M65 S112 030
22 ACCRA 5 684 MG AL2 04
72 ACBCA 28 3533 M65 S116 015
74 ACBCA 30 2467 K6 MG U4
MG+2 V
68 ACSAA 22 1966 M63 P2 08
66 UNPUI 1966 142 MG B4 07
UNPUI MG2 P2 08
UNPUI MG2 P2 07
MG+2 VI
65 CJCHA 43 1130 MG2 P2 07
63 BARCA 11 361 MG2 AS2 07
70 ACBCA 26 1429 MG N H4 P 04
71 CJCHA 49 1010 MG2 P2 07
69 INOCA 8 1665 C54 MG3 F10
69 ZKAKA 129 65 MG S1 U3
65 SPHCA 13 933 M 04
70 JSSCB 2 612 M228 GELIO 0+8
65 MRLMD 1965 1960 MG AL B UN
70 SCIEA 1970 4092 S 04; H2 0
71 ACBCA 27 815 M3 FE 08
68 ACSAA 22 1466 MG2 P2 08
70 REF 1 CA MG S1 04

74 ACBCA 30 2491 M02 V2 07
71 AMMIA 56 1593 MG 186 07 IO H161; 2H2 0
73 AMMIA 58 1029 MG C 03
74 CJCHA 52 1189 M4 B M02 H2 IP 0414
70 INOCA 9 151 MG (IMP4)3 (CL 0412
72 CJCHA 50 3619 MG V2 06
71 ACBCA 29 2611 MG AS2 08
MG+2 VIII
73 ACBCA 29 266 CALCULATED
MH+2 IV
70 AMMIA 55 1489 M27 S8 AS 012
69 ZAACA 369 306 MN V2 04
71 ACBCA 27 1044 MN CO CR 04
69 PHSSA 12 891 MN CR2 04
73 ACBCA 29 266 CALCULATED
MH+2 V HS
68 AMMIA 53 1841 M2 0 H AS 04
74 MPRTA 21 246 M2 AS 04 04
MH+2 VI LS
69 ACBCA 25 925 R VS O ELECTRUMS
MH+2 VI HS
69 SCIEA 165 586 M2 GE 04
69 JCP5A 51 4928 BA MN F4
70 ZKRA 132 1185 IO H12 S12 08
69 AMMIA 54 1312 MN FE2 IP 0412 (H2); 2H2 0
70 NMJIA 113 1 M27 NA12 (S 04113; 15H2 0
65 ACCRA 19 854 MN S 04
72 AMMIA 57 621 M2 GE 04
67 PRLLA 92 125 MN C 03
67 HCACA 50 2023 M25 08
MH+2 VII
72 AMMIA 57 621 M2 GE 04
MH+2 VIII
69 ZKRA 129 427 M3 FE2 GE 012
71 AMMIA 56 791 GARNETS
71 JSSCB 12 109 M3 AL2 GE3 012
74 JCP5A 49 1895 MN B4 07
MH+3 VI HS
21 2871 M2 03
67 ACBCA 124 428 M2 03
68 ACBCA 24 1233 M4 0 D H
69 JCP5A 50 1066 IN H412 MN F5
69 PHSSA 12 891 M2 03
68 BUFGA 91 339 TB MN 03; PR MN 03; NU MN 03
71 JSSCB 3 238 LA MN 03; M3 04
LA S5 CA 05 05
73 JSSCB 6 16 NA M2 012
74 AMMIA 59 985 M2 MN B 05
68 ACBCA 24 1114 M4 M4 T15 018
74 INOCA 13 1854 MN IC7 M5 0213; 1/4 CO HS CH3
74 INOCA 13 1864 MN (ACAC)3
MH+3 IV
73 JSSCB 13 275 R3 VS V (M4 MN 04)
MH+4 VI
73 JSSCB 8 234 BA MN 03
69 INOCA 8 345 NA12 MN NB12 038; 50H2 0
65 CIEPA 11 398 NA4 MN H1 0313; 2H2 0
67 HCACA 50 2023 M25 08; CO2 M3 08
MH+4 IV
28 2845 K2 MN 04
MH+7 IV
68 ACBCA 24 1053 AG MN 04
MH+5 IV
69 ACBCA 25 400 K3 MO CL6
69 INOCA 8 2694 K3 MO F6
MH+4 V
71 MRBUA 6 555 L12 MO F6
MH+5 IV
71 INOCA 13 2715 R3 VS V (RE MO 04)
MH+5 VI
71 INOCA 10 922 BA2 ND MO 06
MH+6 IV
68 JCP5A 48 2619 CU MO 04
68 SPHDA 12 1095 K V M2 08
69 JCSIA 1969 849 K2 MO 04
72 ACBCA 28 60 G2 M01 012
69 JCP5A 50 86 M02 M03 012
71 SPHCA 15 811 L13 FE M02 012
71 SPHCA 15 829 K AL M02 08; K FE M02 08
71 JCP5A 55 1093 CA MO 04; SR MO 04
73 ACBCA 29 2074 LA2 M03 012
71 JCSIA 1971 1857 M01+61 -0
MH+6 V
67 CCJDA 1967 374 K2 M03 010
68 JCSIA 1968 1398 K2 M03 010
MH+6 VI
68 JCSIA 1968 1398 K2 M03 010
70 JSSCB 1 484 AG6 M010 033
70 INOCA 12 1095 K V M2 08
70 ACBCA 28 60 G2 M01 012
70 CCJDA 1970 50 M03 012 H2 012
72 ACBCA 28 2222 M03; 2H2 0
71 INOCA 3 1803 K2 (MO 02 (C2 04) H2 012 0
73 ACBCA 29 869 HG MO 04
74 ACBCA 30 1795 MO 03H2 0
N+3 IV
REF 6 M03 N2; S13 N4; B N; TI N
N+5 III
REF 6 M4 N 03; NA N 03; K N 03;
BAIN 0312; TITIN 0314
NA+1 IV
74 ZAACA 409 69 NA6 ZM 04
REF 2 NA2 0
68 ACBCA 24 1077 NA2 S12 05
68 SPHDA 12 987 NA2 ZN2 S12 07
64 JACSA 329 110 NA2 MG 02
NA+1 VI
70 ACSAA 24 1287 NA4 S2 GE4 012 IO H14
63 ACCRA 15 1233 NA B (OH)4; 2H2 0
60 ZKRA 113 430 NA2 AL2 S13 010; 2H2 0
58 ZKRA 111 241 NA CL 03
56 ACCRA 9 811 INA AS 031X
53 ARKKA 8 77 NA S8 F4
59 ACCRA 12 526 NA U ACETATE
74 ACBCA 30 1872 NA2 M 04
75 ACBCA 31 890 NA2 C 03; H2 0
NA+1 VII
71 SPHCA 15 926 NA GO S1 04
70 NMJIA 113 1 M27 NA12 (S 04113; 15H2 0
73 ACBCA 29 890 NA2 CR2 07 ALPHA
NA+1 VIII
68 ACBCA 24 1703 NA B F4
68 SPHDA 12 987 NA2 ZN2 S12 07
71 AMMIA 56 18 NA3 AL2 L13 F12
NA+1 XII
71 JSSCB 3 89 NA13 NB35 094
62 ZKRA 81 135 NA AL S1 04
NB+3 IV
74 ACIEA 86 819 LI NB 02
75 JACSA 97 2713 NB1DPM14
NB+5 VI
68 JCP5A 48 2619 M27 S8; 5 M2 05; 78
70 JSSCB 1 459 M-2B2 05
70 JSSCB 1 459 M-2B2 05
70 AMMIA 55 90 CA NB2 06
55 PRVAA 98 903 C02 NB2 07
71 JSSCB 3 89 NA13 NB35 094
71 ZAACA 380 119 MN NB2 04
74 JINCA 36 1965 CA2 NB2 07
71 JCSIA 1971 1280 B13 NB17 047

Table 2 (cont.)

72 ACBGA	28	956	BA TB 03		
TC+5 VI					
67 STBGA	3	1	R3 VS V (FLUORIDES)		
TC+7 IV					
69 ACIEA	8	381	TC2 07		
71 ZAACA	380	146	TC2 07		
TE+4 IV					
69 ACCHA	25	1551	H3 PEZ 7E4 012 CL		
71 ACBGA	27	602	71 TE3 08, 3M TE3 08, 7E 02, HF TE3 08, ZR TE3 08		
71 ACBGA	27	608	U TE3 09		
TE+4 VI					
61 ZKXKA	116	365	TE 02		
71 ACBGA	27	602	71 TE3 08		
71 ACBGA	27	608	U TE3 09		
TE+0 IV					
71 JCSIA	1971	1857	TE(+6)+0		
TE+6 VI					
69 ZEMBA	24	647	L16 TE 06		
70 NRUBA	5	189	M03 TE 06		
69 ACSAA	23	3062	NA2 KA TE2 08 10 H12 1H2 0114		
64 INDOA	3	634	K TE 0 10 H15,H2 0		
64 NATMA	51	552	K TE 0 10 H15,H2 0		
66 ACSAA	20	2138	K4 TE2 06 10 H14,H2 0		
70 NATMA	57	393	M03 TE 06		
70 ZAACA	378	129	SR2 MI TE 06		
70 ACSAA	24	3178	TE 10 H16		
66 ACSAA	20	1535	TE F6		
71 ACBGA	27	615	M03 TE 06		
65 ZAACA	334	225	K TE 02 10 H13		
68 CHODA	267	1435	CO2 TE 06		
69 HQCMB	100	1809	AG2 TE 02 10 H14		
71 BUFGA	94	172	TE 10 H16		
73 ACBGA	29	692	TE 06		
73 ACBGA	29	956	H2 TE 06		
73 ACSAA	27	85	TE 10 H16		
74 ACBGA	30	1813	H2 TE 04		
74 ACBGA	30	2095	IN H410 1TE M06 024) TE (0M16 7M2 0		
TH+4 VI					
74 CJCHA	52	2175	R3 VS V		
TH+4 VIII					
71 ACBGA	27	629	K5 TH F9		
71 ACBGA	27	2290	K7 TH F31		
74 ICHAA	8	273	K TH P3 010		
TH+4 IX					
68 CCJDA	1968	990	IN H414 TH F8		
69 ACBGA	25	1958	IN H414 TH F8		
68 CCACA	40	147	K TH P3 012		
70 ICHAA	4	571	NA TH2 (P D+13		
71 ACBGA	27	1823	RB TH F13		
73 ACBGA	29	276	NA BE TH10 F45		
70 ACBGA	26	1185	K NA TH F6		
71 ACBGA	27	2279	IN H413 TH F7		
TH+4 X					
73 ACBGA	29	2687	TH IN 0314 (1C6 H513 P 012		
TH+4 XI					
66 ACCRA	20	842	TH IN 0314,SH2 0		
66 ACCRA	20	836	TH IN 0314,SH2 0		
TH+4 XII					
65 ACCRA	18	698	MG TH IN 0316,8M2 0		
TI+3 VI					
73 JSSCB	6	213	TI 07		
69 PRRVA	130	2230	TI2 03		
74 JSSCB	9	255	TI2 03		
74 ACBGA	30	662	CS TI 15 0412,12M2 0		
TI+4 IV					
71 ACBGA	29	2009	BA2 TI 04		
61 ACCRA	14	875	BA2 TI 04		
71 JCSIA	1971	1857	TI(+4)+0		
74 ZAACA	408	60	RB2 TI 03		
TI+4 V					
68 ACBGA	24	1327	Y2 TI 05		
TI+4 VI					
70 ZKXKA	131	278	Y2 TI2 07		
71 ACBGA	27	635	N2 H6 TI F6		
71 JSSCB	3	340	TI 07		
70 ACACB	40	336	BA TI 03		
64 ACCRA	17	240	CO TI 03		
71 JCPISA	55	3260	TI 02		
1	72	CSCMC	BA TI6 013		
72 ZKXKA	136	273	TI 02		
74 ZKXKA	139	103	K TI P 05		
72 INDOA	11	2989	TI 01C5 H7 021212		
74 ICHAA	11	243	IN H412 TI 01C2 0412,H2 0		
74 ACBGA	30	2894	BA TI2 05		
74 CJCHA	52	2175	R3 VS V		
TI+4 VIII					
66 JCSIA	1966	1496	TI (N 0314 R3 VS V (AF))		
TL+1 VI					
75 ACBGA	31	365	TL N 03		
TL+3 IV					
71 ZAACA	381	129	L15 TL 04		
73 ZAACA	396	113	SR4 TL2 07		
74 ZAACA	405	191	BA2 TL2 05		
TL+3 VI					
68 ZKXKA	126	143	TL2 03		
74 ZAACA	405	197	BA2 TL2 05		
75 ZAACA	412	37	RB TL F4		
TL+3 VIII					
72 ZAACA	393	223	TL F3		
TM+2 VI					
UNPUI			TM 12		
TM+2 VII					
UNPUI			TM CL2,TH BR2		
TM+2 VIII					
63 PHISA	3	K446	TM2 03		
TM+3 VIII					
70 SSGDA	8	1745	TM3 FES 012		
74 ZAACA	403	1	A3 VS V (TM F3)		
TM+3 IX					
74 ZAACA	403	1	A3 VS V (TM F3)		
UN+3 VI					
68 JINCA	30	823	R (U+3)		
UN+4 VI					
73 JSSCB	8	331	R3 VS V		
67 INUGA	3	327	R (U+4)		
74 CJCHA	52	2175	R3 VS V		
UN+4 VIII					
70 ACBGA	26	38	IN H414 U F8		
73 ACBGA	29	1442	U CL4		
UN+4 IX					
69 ACBGA	25	1918	K U2 F0		
69 ACBGA	27	245	C5 U6 F25		
73 ACBGA	29	956	H2 TE 06		
74 ACBGA	30	1906	B - NHA U F5		
UN+5 VI					
67 ACCRA	23	805	CS U F6		
70 JINCA	32	3701	NA U 03		
65 BUFGA	86	214	U CR 04		
67 BUFGA	40	231	U FE U4		
UN+5 VII					
73 SPHCA	18	323	U2 RD 08		
UN+6 VI					
68 ACBGA	24	967	CU U 04		
69 ACBGA	25	787	S U 04, BA U 04, CAZ U 05, SR2 U 05, CA3 U 04,SR3 U 05		
UN+6 VII					
66 JOPDA	27	726	MU U 04		
62 JOPDA	23	677	CO U 04		
65 ACSAA	19	1955	U FA (GAS)		
71 INUGA	7	455	U 03		
71 JINCA	33	2867	CR2 U 06		
72 ACBGA	28	3609	U 02 H12		
73 ACBGA	29	7	U F6		
UN+6 VIII					
72 ACBGA	28	3609	U 03		
UN+6 IX					
69 ACBGA	25	787	CA U 04		
69 ACCRA	19	205	RB U 02 (IN 0313		
V+2 VI					
UNPUS			V F2		
V+3 VI					
70 PRVBA	2	3771	V2 03		
73 JSSCB	6	419	V4 07		
69 ACBGA	25	1354	V IC5 H7 0213		
69 ZAACA	369	306	M V2 04		
74 MRUBA	9	1091	V00,99 CR0,0112 03		
70 JPCSA	31	2569	V2 03		
V+4 V					
65 ACCRA	19	432	L1 V2 05		
61 JCPISA	55	55	V 0 U IC5 H7 0212		
73 ACBGA	29	269	CA V3 07		
73 ACBGA	29	1335	CA V4 09		
V+4 VI					
72 JSSCB	5	446	CU V 03		
73 JSSCB	6	419	V4 07		
72 PRVBA	5	2541	V 02 CR		
74 ACBGA	30	2644	V3 07		
71 ACSAA	25	2075	W6 013		
70 ACSAA	24	420	V02		
74 PRVBA	10	490	V02		
V+4 VII					
68 ACBGA	24	292	V Y 04		
68 CHPLB	2	47	ER V 04		
67 ACCRA	25	240	PH2 V2 08		
70 ZKXKA	131	161	BA3 (V 0412		
71 JSSCB	3	458	RD V 04		
27	71	JSSCB	3	458	RD V 04
70 INDOA	9	2259	CAZ V 04 CL		
71 CJCHA	49	1629	MG V2 08		
73 ACBGA	29	2364	CO1 V2 04, N13 V2 08		
72 JSSCB	4	29	FE V 04		
73 CJCHA	51	1004	ZM2 V2 07		
73 JSSCB	6	538	L13 V 04		
72 CJCHA	50	3944	CU3 V2 08		
71 CJCHA	49	1629	MG V2 08		
73 ACBGA	29	141	V Y 04		
73 ACBGA	29	1338	CU5 V 03		
73 CJCHA	51	264	PH2 V2 08		
74 ACBGA	30	1678	NA V 04		
74 NJMMA	5	210	CA5 (V 0413 0 H		
V+5 V					
50 ACSAA	4	4119	V2 05		
71 KVCMA	8	300	07 05		
74 ACBGA	30	2644	V3 07		
74 ACBGA	30	2491	MG V2 07		
73 ACBGA	29	59	PH2 V2 07		
70 CHODA	270	952	CA V2 06		
V+5 VI					
71 JSSCB	5	432	V P 05		
71 ACSAA	25	2675	W6 013		
72 CJCHA	50	3619	V2 06		
71 CJCHA	49	1629	P 05 ALPHA		
74 CJCHA	52	2184	K3 V 02 C2 04,3M2 0		
73 ACBGA	29	1743	CU V2 06		
V+5 VII					
67 STBGA	3	1	R3 VS V (FLUORIDES)		
M+0 IV					
69 ACBGA	25	1704	K2 M 04		
71 SPHCA	15	636	MD2 M 06		
71 SPHCA	15	928	PB M 06		
62 ACBGA	28	3174	SH 04		
71 JCPISA	55	1093	SR M 04,8M 04		
71 JCSIA	1971	1857			
74 ACBGA	30	1872	NA2 M 04		
74 ACBGA	30	1878	AL2 IN 0413		
M+0 V					
74 ACBGA	30	2587	CA3 M 05 CL2		
M+0 VI					
69 SPHCA	13	933	MG M 04		
69 SSGDA	7	1797	B12 M 06		
70 SPHCA	14	518	K MD IN 0412		
70 SPHCA	14	515	L12 FE (M 0412		
70 SPHCA	15	28	PR2 M 09		
70 ACBGA	26	1020	CU M 04		
70 JSSCB	2	278	L1 FE (M 0412		
66 ACSAA	20	2698	M F6 (GAS)		
72 ZEMBA	27	203	SN M 04		
71 SPHCA	15	991	NO2 M3 015		
74 JSSCB	10	5	FE2 M 06		
74 ACBGA	30	2069	BA W 04		
X+0 IV					
71 JCPISA	52	812	XE 04		
71 JCSIA	1971	1857	XE(+1)+0		
X+0 VI					
64 INDOA	3	1412	NA4 XE 06,8M2 0		
64 INDOA	3	1417	NA4 XE 06,8M2 0		
Y+3 VI					
67 ACBGA	22	354	Y2 BE 04		
68 ZAACA	358	138	SR Y2 04		
67 SPHCA	11	583	NA Y S1 04		
69 ACBGA	25	2140	Y2 03		
71 JCPISA	15	806	Y2 S1 05		
71 JCSIA	1974	229	C66 H12 13 N12 06 Y		
Y+3 VII					
68 INDOA	7	1777	Y(C66)COCH(C6H3)3,H20		
Y+3 VIII					
68 ACBGA	24	292	Y V 04		
57 ACCRA	10	239	Y3 FES 012		
68 SPHCA	12	1095	K Y MD2 08		
69 SPHCA	13	420	K Y W2 08		
70 ZKXKA	131	278	Y2 TI2 07		
67 ACCRA	21	939	Y TA 04		
74 ZAACA	403	1	R3 VS V (Y F3)		
Y+3 IX					
69 ZKXKA	112	362	Y (C2 H5 S 04)3,9H2 0		
74 ZAACA	403	1	R3 VS V (Y F3)		
YB+2 VI					
71 ZAACA	386	221	YB BR2, YB 12		
YB+2 VII					
74 ZAACA	403	4	5 YB CL2		
71 ZAACA	386	221	YB BR2		
YB+2 VIII					
71 ZAACA	386	221	YB F2		
YB+2 VI					
70 SPHCA	14	854	YB2 S1 05		
70 ACBGA	26	984	YB2 S12 07		
70 ZAACA	377	70	CA YB2 04, SR YB2 04		
74 ACBGA	30	1857	YB P3 09		
YB+3 VII					
70 SPHCA	14	854	YB2 S1 05		
69 INDOA	8	22	Y2 YB HT 0213 (H2 0)		
69 INDOA	8	29	YB IC5 HT 0213 (H2 0) 1/2 C6 H6		
YB+3 VIII					
70 INDOA	9	1094	YB L1 F4		
70 SSGDA	8	1745	YB FES 012		
74 MRUBA	9	179	YB P5 014		
74 ZAACA	403	1	R3 VS V (YB F3)		
YB+3 IX					
74 ZAACA	403	1	R3 VS V (YB F3)		
Z+4 IV					
68 SPHDA	12	987	NA2 ZM2 S12 07		
69 ACBGA	25	1233	ZM 04		
69 PHISA	32	K91	ZM FE2 04		
73 ACSAA	27	1541	ZM S 03,2 1/2M2 0		
64 INDOA	3	245	ZM 10PM12		
ZM+2 V					
70 JSSCB	1	120	ZM2 P2 07		
73 CJCHA	51	1004	ZM2 V2 07		
71 AMNIA	56	1147	ZM4 AS2 08 10 H12,2M2 0		
ZM+2 VI					
65 CJCHA	43	1147	ZM2 P2 07		
68 SPHCA	13	127	ZM 04		
70 JSSCB	1	120	ZM2 P2 07		
71 CJCHA	49	3056	ZM3 V2 08		
71 AMNIA	56	1147	ZM4 AS2 08 10 H12,2M2 0		
73 ACBGA	29	2741	ZM S1 F6,8M2 0		
73 ACSAA	27	1541	ZM S 03,2 1/2M2 0		
ZR+4 I					
75 JSSCB	13	275	R3 VS V (M4 ZR 04)		
ZR+4 V					
69 CCJDA	1969	727	K2 ZR 03		
70 JSSCB	2	410	K2 ZR 03		
ZR+4 VI					
69 ACBGA	25	2658	ZR 1H AS 0412,H2 0		
69 ZAACA	371	306	L12 ZR 03		
70 JSSCB	1	478	K2 ZR2 05		
68 ACSAA	22	1822	NA ZR2 P3 012		
73 ACBGA	29	2294	L12 ZR F6		
71 ACBGA	27	1944	R85 ZR F21		
74 CJCHA	52	2175	R3 VS V		
ZR+4 VII					
69 ACBGA	25	2164	NA2 ZR F6		
70 ACBGA	24	417	IN H413 R1 F7		
70 JACTA	53	126	ZR 02		
73 ACSAA	27	177	ZR4 10 H16 (CR 0415,H2 0		
73 ACSAA	27				

compounds to be slightly larger than those of the Eu^{2+} compounds. This difference was assumed to exist for all Sr^{2+} and Eu^{2+} coordinations. Because compounds of Am^{2+} and Sr^{2+} have similar cell volumes, the radius of Am^{2+} was made equal to that of Sr^{2+} .

Wolfe & Newnham (1969) studied $\text{Bi}_{4-x}\text{RE}_x\text{Ti}_3\text{O}_{12}$ and concluded that Bi^{3+} and La^{3+} have nearly equal radii. From a study of BiTaO_4 Sleight & Jones (1975) have concluded that although Bi^{3+} and La^{3+} have essentially equal radii, the size of Bi^{3+} depends on the degree of the $6s^2$ lone-pair character. When BiTaO_4 transforms from a structure where the lone-pair character is dominant to the LaTaO_4 structure, it undergoes a volume reduction. Table 3 shows a comparison of isotopic Bi^{3+} and La^{3+} compounds where the lone-pair character of Bi^{3+} is (1) constrained and (2) dominant. Bi pyrochlores such as $\text{Bi}_2\text{Ru}_2\text{O}_7$, $\text{Bi}_2\text{Ir}_2\text{O}_7$ and $\text{Bi}_2\text{Pt}_2\text{O}_7$ were omitted from the table because no corresponding La pyrochlore exists, but they have unit-cell volumes close to those of the Sm or Nd pyrochlores and thus have smaller volumes than those of La. When Bi^{3+} is forced into high symmetry, a Bi^{3+} compound has a smaller volume than that of La^{3+} , but when the lone-pair character is dominant, the Bi^{3+} compound is distorted and Bi^{3+} and La^{3+} compounds have approximately equal volumes. This behavior was also noted in the highly symmetric garnet structure where the hypothetical $\text{Bi}_3\text{Fe}_3\text{O}_{12}$ was estimated to have cell dimensions between those of the hypothetical $\text{Nd}_3\text{Fe}_3\text{O}_{12}$ and $\text{Pr}_3\text{Fe}_3\text{O}_{12}$ (Geller, Williams, Espinosa, Sherwood & Gilleo, 1963). For practical purposes, Bi^{3+} is listed as slightly smaller than La^{3+} but this dependence on lone-pair character must be kept in mind when comparing the volumes of Bi^{3+} and La^{3+} compounds. Similar behavior may also exist for Pb^{2+} and Sr^{2+} , but this relationship was not investigated.

Table 3. Cell volumes of isotopic Bi^{3+} and La^{3+} compounds

(a) Lone pair character of Bi^{3+} constrained

Compound	Cell volume	Ratio
$\text{BiLi}(\text{MoO}_4)_2$	314.7	0.96
$\text{LaLi}(\text{MoO}_4)_2$	328.7	
$\text{BiNa}(\text{MoO}_4)_2$	320.5	0.97
$\text{LaNa}(\text{MoO}_4)_2$	332.1	
BiOF	87.6	0.90
LaOF	97.7	
BiOCl	110.7	0.95
LaOCl	116.8	
BiOBr	123.8	0.98
LaOBr	126.4	
BiPO_4	293.0	0.96
LaPO_4	304.7	

(b) Lone pair character of Bi^{3+} dominant

Bi_2MoO_6	268.5 ($\times 8$)	1.00
La_2MoO_6	267.3	
BiFeO_3	62.49 ($\times 6$)	1.03
LaFeO_3	60.77 ($\times 4$)	
$\text{Bi}_2\text{Sn}_2\text{O}_7$	1219.9 ($\times 8$)	1.00
$\text{La}_2\text{Sn}_2\text{O}_7$	1225.3	

A similar study of relative cell volumes of isotopic compounds involving the pairs Cu^+-Li^+ , Ag^+-Na^+ , Tl^+-Rb^+ , and $\text{Pb}^{2+}-\text{Sr}^{2+}$ was used to obtain more reliable estimates of the radii of Cu^+ , Ag^+ , Tl^+ , and Pb^{2+} (Shannon & Gumerman, 1975).

The nature of Sn^{2+} , NH_4^+ , and H^- made it impossible to define their ionic radii. The coordination of Sn^{2+} by oxygen or fluorine is always extremely irregular,* leading to average distances which depend on the degree of distortion. Since this distortion varies widely from one compound to another, it is not meaningful to define an ionic radius.

Khan & Baur (1972) derived an apparent radius of the NH_4^+ ion by analyzing the N-O distances in a large number of ammonium salts. They concluded that NH_4^+ has an octahedral radius of 1.61 Å, between that of Rb^+ (1.52 Å) and Cs^+ (1.67 Å). Alternatively, cell volumes of NH_4^+ and Rb^+ fluorides, chlorides, bromides, iodides and oxides may be compared. This leads to the conclusion that NH_4^+ is not significantly different in size from Rb^+ . No explanation is offered for this inconsistency and therefore the radius of NH_4^+ is not included.

The radius of the hydride ion, H^- , has been the subject of some controversy. A number of different radii have been proposed: 2.08 (Pauling, 1960); 1.40 (Gibb, 1962); and 1.53 Å (Morris & Reed, 1965). Gibb studied interatomic distances in many hydrides and concluded that good agreement between observed and calculated distances could be obtained using $r(\text{VIH}^-) = 1.40$ Å if corrected for cation and anion coordination. The value of $r(\text{IVH}^-)$ was taken to be 1.22 Å.

Morris & Reed (1965) concluded that differences in observed distances in hydrides were caused by the large H^- polarizability. Because of such wide variations in the apparent H^- radius, it was omitted. However, an explanation for the variations based on covalence differences will be discussed later.

* Although cell dimensions of $\text{Sn}_2\text{M}_2\text{O}_7$ pyrochlores were used in SP 69 to derive $r(\text{VIISn}^{2+})$, Stewart, Knop, Meads & Parker (1973) and Birchall & Sleight (1975) recently found that the pyrochlore A site in $\text{Sn}_2\text{Ta}_2\text{O}_7$ is not fully occupied. Thus, even this example of apparently regular Sn^{2+} polyhedra is not valid.

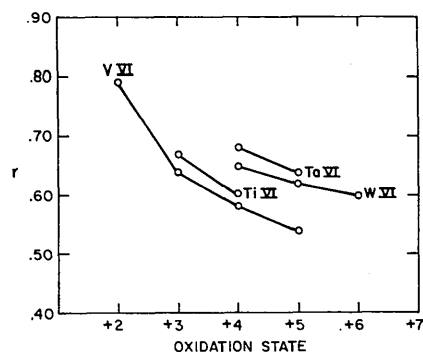
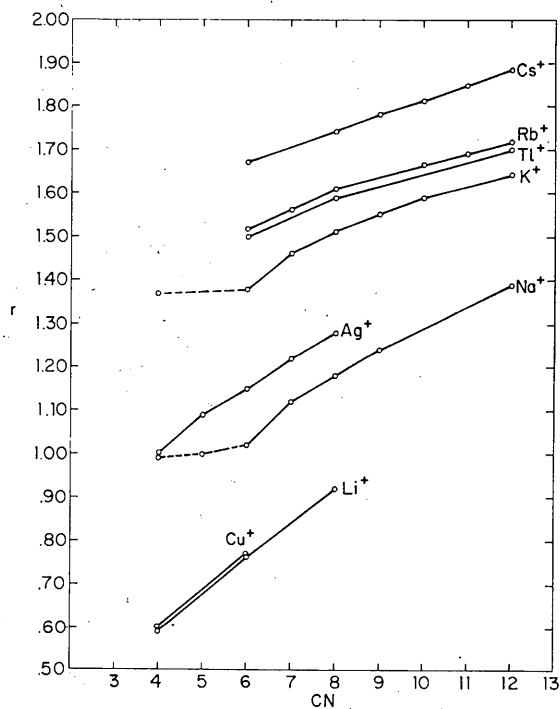


Fig. 1. Effective ionic radius (Å) vs oxidation state.

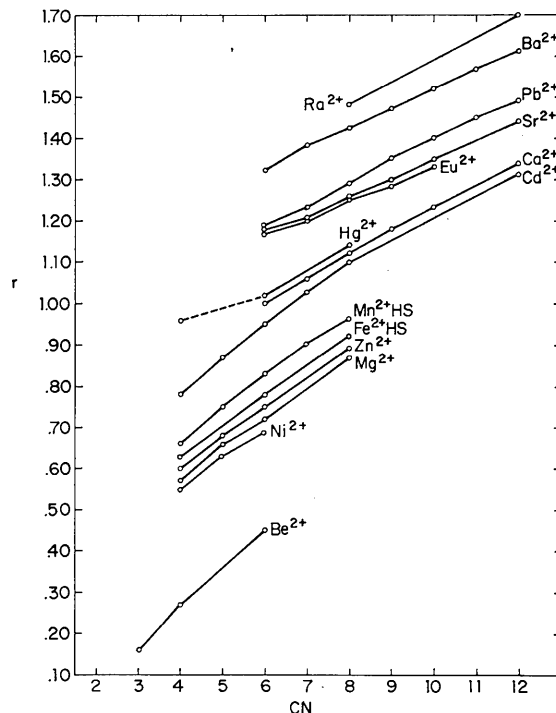
Results and discussion

In Table 1 two sets of radii are included. The first is a set of traditional radii based on $r(\text{VI}\text{O}^{2-}) = 1.40 \text{ \AA}$. The

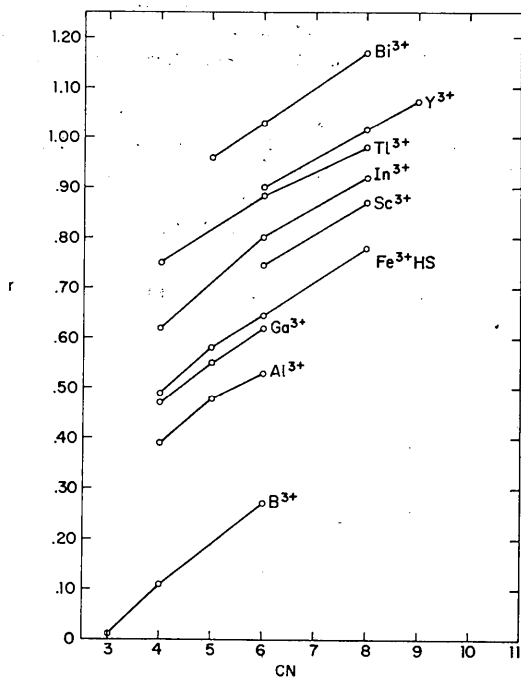
other set is based on $r(\text{VI}\text{O}^{2-}) = 1.26$ and $r(\text{VI}\text{F}^-) = 1.19 \text{ \AA}$, and corresponds to crystal radii as defined by Fumi & Tosi (1964). As pointed out in SP 69, crystal radii differ from traditional radii only by a constant factor



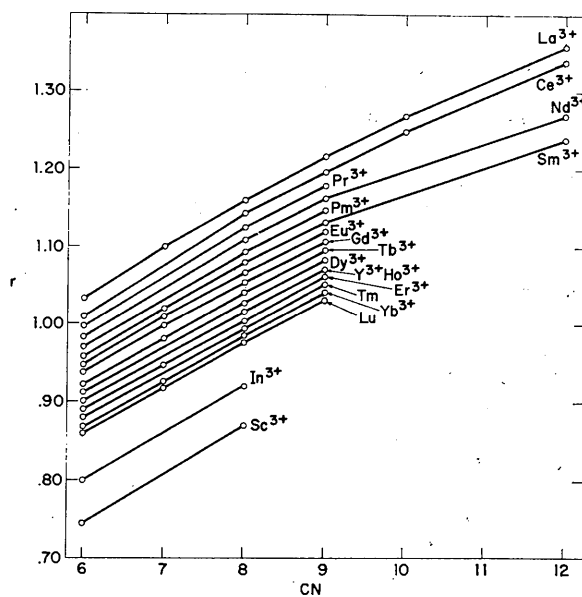
(a)



(b)

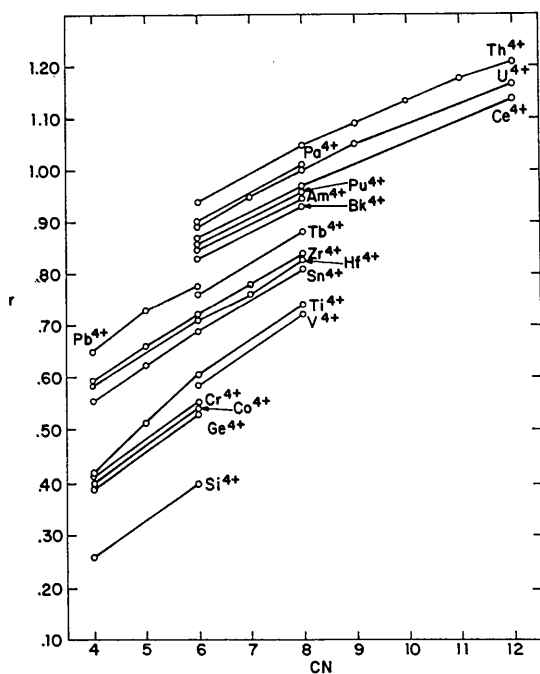


(c)



(d)

Fig. 2. (a)–(e) Effective ionic radius (Å) vs CN for some common cations.



(e)

Fig. 2. (cont.)

of 0.14 Å. Although their inclusion in Table 1 may seem superfluous, it is felt that crystal radii correspond more closely to the physical size of ions in a solid. They should be used, for example, in discussions of closest packing of spheres, structure field maps (Muller & Roy, 1974), and diffusion in solids (Flygare & Huggins, 1973). Traditional radii have been retained because of their familiarity to crystal chemists and physicists. They will probably continue to be used for comparison of unit-cell volumes and interatomic distances. In the table, the ion is followed by electron configuration (EC), coordination number (CN), spin state (SP), crystal radius (CR), and effective ionic radius (IR), and in the last column, a symbol indicating the derivation of the radii and their reliability. Those with a question mark are doubtful because of: uncertainty in CN, or deviation from radii *vs* CN, or radii *vs* valence plots. Where at least five structural determinations resulted in radii differing by no more than ± 0.01 Å, the values are marked with an asterisk.

When the choice of a radius was influenced by any of the various correlations described earlier, it is indicated by the following: *R* – from r^3 *vs* unit cell volume plots; *C* – calculated from bond length–bond strength equations; *E* – estimated from one or more plots of *r* *vs* valence, *r* *vs* CN, and *r* *vs* cell volume. *E* implies poor or nonexistent structural data. Radii in this category include ${}^{\text{VI}}\text{Fe}^{2+}\text{LS}$, ${}^{\text{VI}}\text{Mn}^{2+}\text{LS}$, ${}^{\text{VI}}\text{Cr}^{2+}\text{LS}$, ${}^{\text{VI}}\text{V}^{2+}$, ${}^{\text{VI}}\text{Ni}^{3+}\text{HS}$, ${}^{\text{VI}}\text{Ir}^{3+}$, ${}^{\text{VI}}\text{Mo}^{3+}$, ${}^{\text{VI}}\text{Ta}^{3+}$, ${}^{\text{VI}}\text{Pa}^{3+}$, ${}^{\text{VI}}\text{Ta}^{4+}$, ${}^{\text{IV}}\text{Pb}^{4+}$, ${}^{\text{VI}}\text{Ir}^{5+}$, ${}^{\text{VI}}\text{Os}^{5+}$, ${}^{\text{VI}}\text{Re}^{5+}$, ${}^{\text{VI}}\text{Pu}^{5+}$, ${}^{\text{VI}}\text{Bi}^{5+}$,

${}^{\text{VI}}\text{Os}^{6+}$, ${}^{\text{VI}}\text{Re}^{6+}$, and ${}^{\text{VI}}\text{Os}^{7+}$. The symbol *A* means that Ahrens (1952) ionic radius was used whereas *P* means Pauling's (1960) crystal radius was used. The symbol *M* means that the radius was derived from a compound having metallic conductivity. Distances calculated from these radii may be too small for use in compounds having localized electrons. (See discussion *Effects of electron delocalization*.)

In addition, the sources of the radii are indicated in Table 2.

Fig. 2(a)–(e) shows that *r*–CN plots are reasonably regular. Notable exceptions are ${}^{\text{IV}}\text{Na}^+$, ${}^{\text{V}}\text{Na}^+$, and ${}^{\text{IV}}\text{K}^+$. It is apparent that Na–O and K–O distances do not decrease as much as anticipated from the *r*–CN curve* when the CN falls below six. Typical distances and corresponding radii in Table 4 show that Na–O distances in four-coordination are only slightly less than in six-coordination. The reduction in interatomic distances is caused primarily by the decreased repulsive forces due to fewer ligands according to the expression of Pauling (1960):

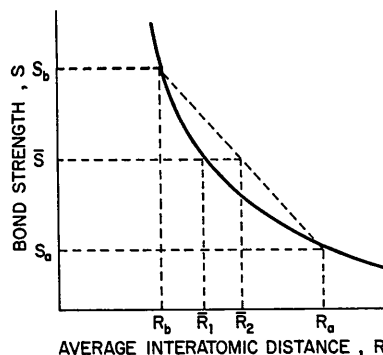
$$\frac{R_{\text{CsCl}}}{R_{\text{NaCl}}} = \left[\frac{A_{\text{NaCl}}}{A_{\text{CsCl}}} \frac{B_{\text{CsCl}}}{B_{\text{NaCl}}} \right]^{1/(n-1)}$$

where *R* = interatomic distance, *A* = Madelung constant, *B* = the cation CN and *n* = Born repulsion coefficient. It appears that this equation is not valid for four-coordinated Na^+ or K^+ .

There are a few small irregularities in *r*–CN plots probably caused by poor or insufficient data, *e.g.* curves for Ti^{3+} *vs* Y^{3+} . The differences in slopes of Ti^{4+} *vs* Cr^{4+} and V^{5+} *vs* As^{5+} are probably caused by Ti^{4+} –O and V^{5+} –O octahedra being generally more distorted, which leads to greater average interatomic distances.

It is also interesting to compare distances in square planar coordination *versus* tetrahedral coordination. Radii of square planar Cu^{2+} and Ag^+ are equal to or slightly greater than corresponding tetrahedral radii, consistent with the trend anticipated from anion

* Extrapolation of the Na curve gives $r({}^{\text{IV}}\text{Na}^+) = 0.90$ Å.

Fig. 3. Typical bond length *vs* bond strength plot.

repulsion effects. A similar comparison with Fe^{2+} and Ni^{2+} cannot be made because of electron distribution changes from tetrahedral to square planar coordination.

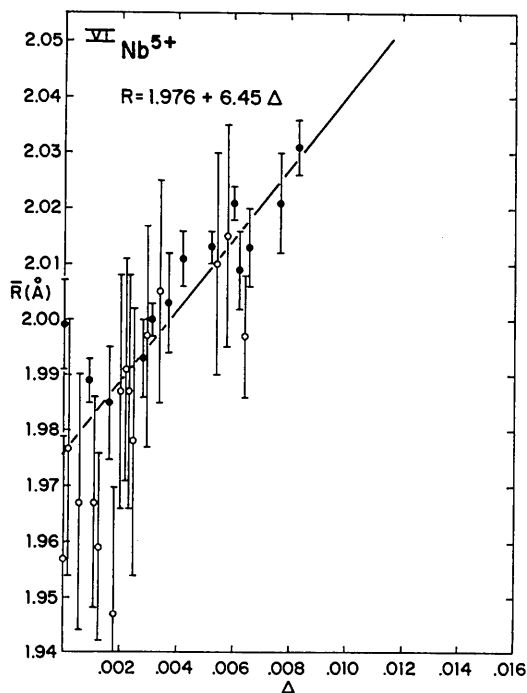


Fig. 4. Mean Nb^{5+} -O bond length *vs* distortion. Vertical bars represent average e.s.d.'s quoted by the authors. Solid circles represent more accurate data.

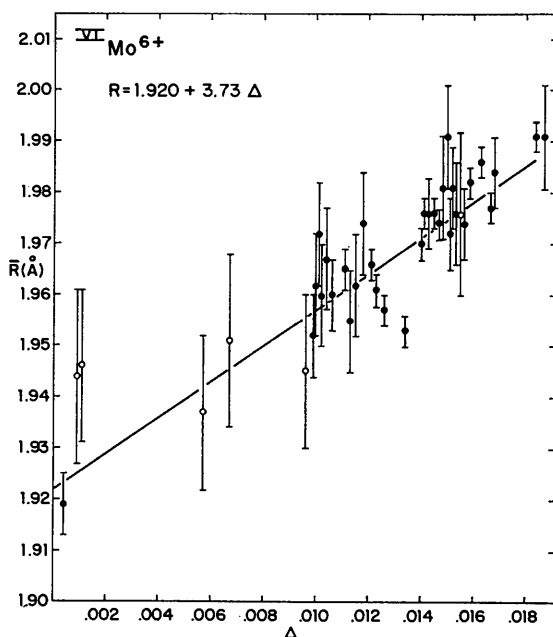


Fig. 5. Mean Mo^{6+} -O bond length *vs* distortion.

Table 4. *Interatomic distances in some compounds containing tetrahedral and octahedral Na^+*

Compound	\bar{R} (Å)	r (Å)	Reference
(a) IVNa^+			
Na_2O	2.40	1.02	
$\text{Na}_5\text{P}_3\text{O}_{10}$	2.37	0.99	60 ACCRA 13 263
$\text{NaOH} \cdot \text{H}_2\text{O}$	2.36	1.00	57 ACCRA 10 462
Na_6ZnO_4	2.39	0.99	69 ZAACA409 69
Mean	2.38	1.00	
(b) VI Na^+			
Na_2WO_4	2.38	1.00	74 ACBCA 30 1872
$\text{NaC}_6\text{O}_7\text{H}_7$	2.37	1.01	65 ACCRA 19 561
$\text{Na}_4\text{Sn}_2\text{Ge}_4\text{O}_{12}(\text{OH})_4$	2.39	1.02	70 ACSAA 24 1287
$\text{Na}_2\text{P}_2\text{O}_7 \cdot 10\text{H}_2\text{O}$	2.48	1.10	64 ACCRA 17 672
NaHCO_3	2.44	1.06	65 ACCRA 18 818
$\text{Na}_2\text{B}_4\text{O}_6(\text{OH})_2 \cdot 3\text{H}_2\text{O}$	2.41	1.04	67 SCIEA 154 1453
$\text{Na}_4\text{P}_4\text{O}_{12} \cdot 4\text{H}_2\text{O}$	2.415	1.05	61 ACCRA 14 555
$\text{NaAl}(\text{SO}_4)_2 \cdot 12\text{H}_2\text{O}$	2.45	1.10	67 ACCRA 22 182
$\text{NaB}(\text{OH})_4 \cdot 2\text{H}_2\text{O}$	2.460	1.09	63 ACCRA 16 1233
NaU acetate	2.375	1.025	59 ACCRA 12 526
$\text{C}_{10}\text{H}_{13}\text{N}_5\text{NaO}_6\text{P} \cdot 6\text{H}_2\text{O}$	2.406	1.046	75 ACBCA 31 19
Mean	2.42	1.05	

Factors affecting mean interatomic distances

Additivity of radii to give mean interatomic distances is not so important to the synthetic chemist who is primarily interested in ionic radii for predicting substitution in crystal structures. Crystallographers and physicists, however, are concerned with comparing calculated and experimental interatomic distances and predicting distances, *e.g.* for distance least-squares (DLS) structure refinements (Baur, 1972; Tillmanns, Gebert & Baur, 1973; Dempsey & Strens, 1975). The effective ionic radii in Table 1 can be used to reproduce moderately well most average interatomic distances in oxides and fluorides. However, certain deviations do occur. Some of these are unexplained but others can be attributed to (1) polyhedral distortion, (2) covalence, (3) partial occupancy of cation sites, or (4) electron delocalization.

1. Polyhedral distortion

To see the effects of polyhedral distortion consider the relationship between bond length (R) and Pauling bond strength (s) (Brown & Shannon, 1973). The analytical expression $s = s_0(R/R_0)^{-N}$, where s_0 is an ideal bond strength associated with R_0 , and R_0 and N are fitted parameters, was evaluated for cation-oxygen pairs for the first three rows of the periodic table. Using these relationships, the sums of bond strengths about cations and anions were found to equal the valences with a mean deviation of about 5%. Accepting the approximate validity of Pauling's second rule, $p = \sum s$ where $p = \text{valence}$, it is possible to derive the effects of distortion of various polyhedra on their mean bond distances. Fig. 3 shows a typical R - s curve. An undistorted octahedron results in an average bond strength \bar{s} and a mean distance \bar{R}_1 . A distorted octahedron with three bonds of length R_a and three of length R_b results in the same average bond strength, \bar{s} , but a mean distance $\bar{R}_2 > \bar{R}_1$.

The effects of distortion on mean bond lengths in numerous polyhedra have been determined. Although distortions in tetrahedra are not as important as in octahedra, they can contribute to variations in mean tetrahedral distances (Baur, 1974; Hawthorne, 1973). Strongly distorted octahedra like those containing V^{5+} , Cu^{2+} , and Mn^{3+} show a significant variation in mean distance with distortion, Δ^* (Brown & Shannon, 1973; Shannon & Calvo, 1973a; Shannon, Gumerman & Chenavas, 1975). Octahedra containing Mg^{2+} , Zn^{2+} , Co^{2+} , and Li^+ are generally less distorted than those of V^{5+} , Cu^{2+} , and Mn^{3+} and show a less pronounced dependence on mean bond length (Brown & Shannon, 1973).

The effects of distortion on mean bond lengths in $Nb^{5+}-O$ and $Mo^{6+}-O$ octahedra are illustrated in Figs. 4 and 5. Tables 5 and 6 list the data used to derive the figures.

Table 7 lists the results of linear regression analyses of mean bond length on distortion for all octahedra studied. It is clear from Fig. 4 that undistorted Nb^{5+} octahedra in pyrochlores have a distinctly smaller mean value than in compounds like $NbOPO_4$, $CaNb_2O_6$, and Na_3NbO_4 . Most of the accurately refined molybdates have relatively distorted octahedra. However, certain ordered perovskites with no octahedral distortion such as Ba_2CaMoO_6 would be expected to have much smaller mean $Mo^{6+}-O$ distances than a typical molyb-

date. In fact, the $Mo^{6+}-O$ octahedra in $Mo_2(O_2C_6Cl_4)_6$ with a very small distortion have the short mean distance of 1.919 Å.

Table 7 also lists the results of regression analyses for $Ta^{5+}-O$ and $W^{6+}-O$ octahedra but they are only approximate because of the scarcity of accurate structural data. Analysis of $Ti^{4+}-O$ octahedra was unsuccessful because of scatter in the data. Distances in $Ba_6Ti_{17}O_{40}$ (Tillmanns & Baur, 1970) and $BaTiO_3$ (Evans, 1951) deviated significantly from a linear relation.

Relations between mean distance and distortion should be particularly useful to help determine oxidation states in mixed valence compounds with such combinations as $Mo^{5+}-Mo^{6+}$, $W^{5+}-W^{6+}$, $V^{4+}-V^{5+}$, $Nb^{4+}-Nb^{5+}$ and $Mn^{3+}-Mn^{4+}$. Such considerations helped rationalize $Mn-O$ distances in $NaMn_7O_{12}$ and the mineral pinakiolite (Shannon, Gumerman & Chenavas, 1975).

The radii in Table 1 are generally derived for an average degree of distortion. Thus, interatomic distances calculated from these radii may be inaccurate if the distortion in a particular compound is much less or greater than usual. This applies particularly to cations whose polyhedra frequently show a large distortion, e.g. Mo^{6+} , Nb^{5+} , V^{5+} , Ba^{2+} , and the alkali ions.

2. Effects of partial occupancy of cation sites on mean cation-anion distances

In compounds with partially occupied sites, abnormally large cation-anion distances are usually found, as expected if the anions surrounding unoc-

* Octahedral distortion is defined by $\Delta = \frac{1}{6} \sum (R_i - \bar{R}/\bar{R})^2$ where \bar{R} = average bond length and R_i = an individual bond length.

Table 5. Comparison of mean octahedral $Nb^{5+}-O$ distances with distortion

Only structures with e.s.d.'s for $Nb-O$ distances of < 0.025 Å were used.

Compound	\bar{R} (Å)	Distortion $\Delta = \langle (\Delta R/R)^2 \rangle \times 10^4$	Reference	
Hg ₂ Nb ₂ O ₇	1.999	0	68 INOCA	7 1704
Cd ₂ Nb ₂ O ₇	1.957	0	72 CJCHA	50 3648
Na ₂ Nb ₄ O ₁₁	1.977	1	70 JSSCB	1 454
Ba _{0.27} Sr _{0.75} Nb ₂ O _{5.78}	1.967	6	61 JCPSA	48 5048
Na ₁₃ Nb ₃₅ O ₉₄	1.965	7	71 JSSCB	3 89
Ba ₃ Si ₄ Nb ₆ O ₂₆	1.989	9	70 ACBCA	26 102
Na ₁₃ Nb ₃₅ O ₉₄	1.967	11	71 JSSCB	3 89
Na ₁₃ Nb ₃₅ O ₉₄	1.959	12	71 JSSCB	3 89
Na ₁₃ Nb ₃₅ O ₉₄	1.964	12	71 JSSCB	3 89
NaNbO ₃	1.985	16	69 ACBCA	25 851
Na ₁₃ Nb ₃₅ O ₉₄	1.947	18	71 JSSCB	3 89
Na ₁₃ Nb ₃₅ O ₉₄	1.991	22	71 JSSCB	3 89
Na ₁₃ Nb ₃₅ O ₉₄	1.987	22	71 JSSCB	3 89
Na ₁₃ Nb ₃₅ O ₉₄	1.978	24	71 JSSCB	3 89
LiNb ₅ O ₈	1.993	28	71 ACSAA	25 3337
LiNbO ₃	2.000	31	66 JPCSA	27 997
Ca ₂ Nb ₂ O ₇	1.997	31	74 JINCA	36 1965
Ca ₂ Nb ₂ O ₇	2.005	34	74 JINCA	36 1965
SbNbO ₄	2.003	37	65 CCJDA	1965 611
KNbO ₃	2.011	42	67 ACACA	22 639
Na ₃ NbO ₄	2.013	52	74 BUFGA	97 3
Ca ₂ Nb ₂ O ₇	2.010	53	74 JINCA	36 1965
Ca ₂ Nb ₂ O ₇	2.015	58	74 JINCA	36 1965
Na ₃ NbO ₄	2.021	60	74 BUFGA	97 3
CaNb ₂ O ₆	2.021	76	70 AMMIA	55 90
GaNbO ₄	2.031	83	65 ACACA	18 874

Table 6. Comparison of mean octahedral Mo⁶⁺-O distances with distortion

Only structures with e.s.d.'s for Mo-O distances of <0.025 Å were used.

Compound	\bar{R} (Å)	Distortion		Reference	
		$\Delta = \langle (\Delta R/R)^2 \rangle \times 10^4$			
Mo ₂ (O ₂ C ₆ Cl ₄) ₆	1.919	5	75 JACSA	97	2123
Mo ₄ O ₁₁ orthorhombic	1.944	9	63 ARKEA	21	365
Mo ₄ O ₁₁ monoclinic	1.946	10	63 ARKEA	21	365
Mo ₄ O ₁₁ monoclinic	1.937	56	63 ARKEA	21	365
Mo ₄ O ₁₁ orthorhombic	1.951	67	63 ARKEA	21	365
Mo ₄ O ₁₁ orthorhombic	1.911	96	63 ARKEA	21	365
Mo ₄ O ₁₁ monoclinic	1.945	96	63 ARKEA	21	365
(C ₁₅ H ₁₁ O ₂) ₂ MoO ₂	1.952	99	74 ACBCA	30	300
(NH ₄) ₆ [Mo ₇ O ₂₄].4H ₂ O	1.962	99	75 JCSIA	1975	505
(NH ₄) ₆ [Mo ₇ O ₂₄].4H ₂ O	1.972	101	75 JCSIA	1975	505
(NH ₄) ₆ [Mo ₇ O ₂₄].4H ₂ O	1.960	104	75 JCSIA	1975	505
LiMoO ₂ AsO ₄	1.967	104	70 ACSAA	24	3711
(NH ₄) ₆ Mo ₈ O ₂₇ .4H ₂ O	1.960	106	74 ACBCA	30	48
HgMoO ₄	1.965	111	73 ACBCA	29	869
(NH ₄) ₆ [Mo ₇ O ₂₄].4H ₂ O	1.955	113	75 JCSIA	1975	505
(NH ₄) ₆ [Mo ₇ O ₂₄].4H ₂ O	1.962	115	75 JCSIA	1975	505
(NH ₄) ₆ [Mo ₇ O ₂₄].4H ₂ O	1.974	118	68 JACSA	90	3275
MoO ₃ .2H ₂ O	1.966	121	72 ACBCA	28	2222
MoO ₃ .2H ₂ O	1.961	123	72 ACBCA	28	2222
MoO ₃ .2H ₂ O	1.957	126	72 ACBCA	28	2222
MoO ₃ .2H ₂ O	1.953	134	72 ACBCA	28	2222
(NH ₄) ₅ [MoO ₃] ₅ (PO ₄)(HPO ₄)].3H ₂ O	1.970	140	74 JCSIA	1974	941
Na ₃ (CrMo ₆ O ₂₄ H ₆).8H ₂ O	1.976	141	70 INOCA	9	2228
(NH ₄) ₆ Mo ₈ O ₂₇ .4H ₂ O	1.976	141	74 ACBCA	30	48
Na ₃ CrMo ₆ O ₂₄ H ₆ .8H ₂ O	1.976	143	70 INOCA	9	2228
(NH ₄) ₅ [(MoO ₃) ₅ (PO ₄)(HPO ₄)].3H ₂ O	1.974	145	74 JCSIA	1974	941
(NH ₄) ₆ [TeMo ₆ O ₂₄].Te(OH) ₆ .7H ₂ O	1.981	147	74 ACBCA	30	2095
CoMoO ₄	1.991	150	65 ACACA	19	269
(NH ₄) ₆ Mo ₈ O ₂₇ .4H ₂ O	1.972	151	74 ACBCA	30	48
MoO ₃	1.981	151	63 ARKEA	21	357
(NH ₄) ₆ [Mo ₇ O ₂₄].4H ₂ O	1.976	152	68 JACSA	90	3275
K ₂ {[MoO ₂ (C ₂ O ₄)(H ₂ O)] ₂ O}	1.976	152	64 INOCA	3	1603
(NH ₄) ₆ Mo ₈ O ₂₇ .4H ₂ O	1.974	152	74 ACBCA	30	48
(NH ₄) ₅ [(MoO ₃) ₅ (PO ₄)(HPO ₄)].3H ₂ O	1.982	159	74 JCSIA	1974	941
Na ₃ CrMo ₆ O ₂₄ H ₆ .8H ₂ O	1.986	163	70 INOCA	9	2228
(NH ₄) ₅ [(MoO ₃) ₅ (PO ₄)(HPO ₄)].3H ₂ O	1.977	167	74 JCSIA	1974	941
MoO ₃ .H ₂ O	1.984	167	74 ACBCA	30	1795
(NH ₄) ₅ [(MoO ₃) ₅ (PO ₄)(HPO ₄)].3H ₂ O	1.991	186	74 JCSIA	1974	941
(NH ₄) ₆ [Mo ₇ O ₂₄].4H ₂ O	1.991	189	75 JCSIA	1975	505
(NH ₄) ₆ [Mo ₇ O ₂₄].4H ₂ O	2.008	197	75 JCSIA	1975	505

Table 7. Variation of mean M-O distance and effective ionic radius in octahedral environments as a function of distortion

Ion	Maximum $\Delta \times 10^4$	N*	R ₀ †	r ₀ ‡	m	Correlation coefficient	Goodness of fit (× 10 ³)
Mo ⁶⁺	212	38	1.920		3.73	0.74	67
				0.572	3.01	0.63	70
W ⁶⁺	122	7	1.925		3.30	0.75	19
				0.565	3.28	0.66	24
V ⁵⁺	576	16	1.887		2.62	0.98	8
Nb ⁵⁺	83	29	1.976		6.45	0.69	71
				0.599	6.83	0.44	99
Ta ⁵⁺	79	6	1.984		6.70	0.81	18
				0.617	3.79	0.15	46
Mn ³⁺	71	15	1.994		7.08	0.82	30
				0.624	6.15	0.54	50
Cu ²⁺	316	26	2.085		3.99	0.82	77
Mg ²⁺	156	28	2.094		8.31	0.72	21
				0.728	8.86	0.77	18
Co ²⁺	46	15	2.106		7.38	0.42	19
				0.734	11.70	0.70	16
Zn ²⁺	71	16	2.099		7.70	0.64	21
				0.736	8.20	0.74	16
Li ⁺	148	11	2.159		8.42	0.81	30
				0.784	9.02	0.79	35

* N = number of independent octahedra

† R = R₀ + mΔ.‡ r = r₀ + mΔ.

cupied sites relax toward their bonded cation neighbors. Therefore average distances should increase as the occupancy factor decreases. In general, partial occupancy seems to be more prevalent for cations which are weakly bonded to oxygen like Cu^+ , Ag^+ , alkali ions, and large alkaline earths. The most prominent examples are Li and Na compounds. Table 8 summarizes the existent data on some structures with partial cation occupancy. Fig. 6 shows the dependence of mean Li–O bond length on the degree of occupancy. Although the data are not extensive, it is apparent that mean distance increases as occupancy factor decreases. Extrapolation of the Li curve in Fig. 6 to zero occupancy, *i.e.* a tetrahedral Li vacancy, gives 2.10–2.15 Å, which is close to the 2.11 Å found for $\alpha\text{-Li}_5\text{GaO}_4$ by Stewner & Hoppe (1971) and for β eucryptite by Tscherry, Schulz & Laves (1972).

Another example of the effects of partial occupancy can be found in the non-stoichiometric feldspar $\text{Sr}_{0.84}\text{Na}_{0.03}\text{Al}_{1.69}\text{Si}_{2.29}\text{O}_8$ reported by Grundy & Ito (1974). The mean Sr–O distance in this compound is 0.03 Å greater than in the stoichiometric $\text{SrAl}_2\text{Si}_2\text{O}_8$ (Chiari, Calleri, Bruno & Ribbe, 1975).

The relation between mean distance and occupancy probably cannot be quantified precisely because the relaxation of oxygen ions will depend on the nature and number of other cation neighbors.

3. Effects of covalence

Changes in interatomic distances due to covalence effects are anticipated in compounds with (1) anions less electronegative than fluorine or oxygen, *i.e.* chlor-

ides, bromides, sulfides, selenides, *etc.* and (2) tetrahedral oxyanions such as the VO_4^{3-} and AsO_4^{3-} groups. The effects of covalence show up as a lack of additivity of the radii and are generally referred to as ‘covalent shortening’.

(a) *Halides and chalcogenides.* Covalence effects can be observed by comparing the relative contraction of cation–anion distances in two different isotypic compounds as the anion becomes less electronegative, *e.g.* Fe^{2+} in Fe_2GeO_4 and Fe_2GeS_4 vs Mg^{2+} in Mg_2GeO_4 and Mg_2GeS_4 . Covalence shortens both Fe–S and Mg–S bonds relative to Fe–O and Mg–O bonds, but because of the greater electronegativity of Fe^{2+} (1.8) compared to Mg^{2+} (1.2), the Fe–S bonds are shortened to a greater extent. Thus a ‘covalency contraction’ parameter (Shannon & Vincent, 1974) can be defined:

$$R_d = \frac{d(\text{Fe-X})^3}{d(\text{Mg-X})^3}$$

where $d(\text{Fe-X})$ = mean Fe–X distance.

A similar parameter

$$R_v = \frac{V(\text{Fe}_m\text{X}_n)}{V(\text{Mg}_m\text{X}_n)}$$

compares the volume of an Fe^{2+} compound with that of an isotypic Mg^{2+} compound. To see the effects of covalence on the Fe–X distance relative to the Mg–X distance, the ratio R_v or R_d may be plotted against the difference in electronegativity of the Fe–X bond, $\Delta\chi_{\text{Fe-X}}$. Such schematic R_v – $\Delta\chi$ plots are shown in Fig. 7. The reference ions for Cd^{2+} and In^{3+} are Ca^{2+} and Sc^{3+} respectively. Such plots usually show a strong

Table 8. Mean distances in structures with partially occupied cation sites

Compound	Occupancy factor	\bar{R}	Reference		
(a) IVLi^+					
Typical	1.00	1.97	Table 1		
LiAlSiO_4 (β eucryptite)	1.00	2.020 (4)	73 AMMIA	58	681
		2.025 (7)	72 ZKKKA	135	175
$\text{LiAlSi}_2\text{O}_6$ II (β spodumene)	0.50	2.08 (4)	68 ZKKKA	126	46
		2.085 (9)	69 ZKKKA	130	420
LiAlSiO_4 (β eucryptite)	0.50	2.056 (2)	72 ZKKKA	135	161
$\text{Li}_2\text{Al}_2\text{Si}_3\text{O}_{10}$	0.40	2.064 (4)	70 ZKKKA	132	118
$\text{LiAlSi}_2\text{O}_6$ III	0.33	2.068 (5)	68 ZKKKA	127	327
$\alpha\text{-Li}_5\text{GaO}_4$	0.00	2.11	71 ACBCA	27	616
LiAlSiO_4	0.00	2.11	72 ZKKKA	135	175
(b) VI Na^+					
Typical	1.00	2.42	Table 1		
$\text{Na}_2\text{Fe}_2\text{Al}(\text{PO}_4)_3$ (wylieite)	0.91	2.533 (6)	74 AMMIA	59	280
NaSbO_3	0.82	2.74	74 JSSCB	9	345
$\text{Na}_2\text{Fe}_2\text{Al}(\text{PO}_4)_3$ (wylieite)	0.70	2.723 (6)	74 AMMIA	59	280
$\text{NaAlSi}_3\text{O}_8$ (high albite)	0.50	2.600 (9)	69 ACBCA	25	1503
$\text{NaAl}_{11}\text{O}_{17}$ ($\beta\text{-Al}_2\text{O}_3$)	0.35	2.839 (1)	68 ZKKKA	127	94
NaSbO_3	0.29	2.65	74 JSSCB	9	345
$\text{Na}_{2.58}\text{Al}_{21.81}\text{O}_{34}$ ($\beta\text{-Al}_2\text{O}_3$)	0.25	2.88	71 ACBCA	27	1826
(c) VI Ag^+					
Typical	1.00	2.50	Table 1		
AgSbO_3	0.44	2.64	74 JSSCB	9	345
AgSbO_3	0.33	2.75	74 JSSCB	9	345
$\text{Ag}_{2.4}\text{Al}_{22}\text{O}_{34.2}$	0.22	2.83	72 JSSCB	4	60

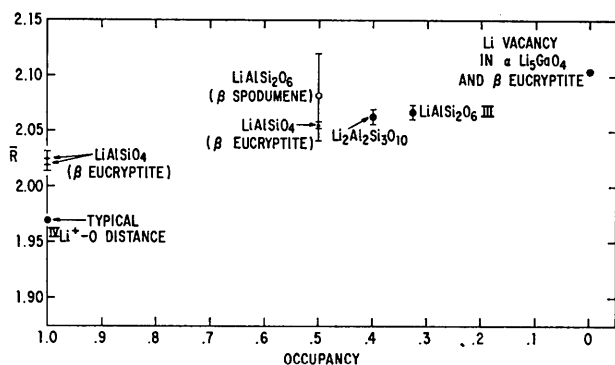


Fig. 6. Mean $\text{Li}^+\text{-O}$ bond length vs partial occupancy.

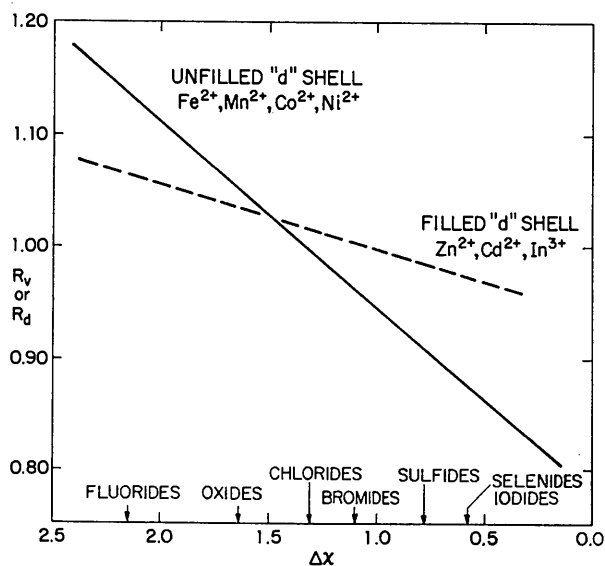


Fig. 7. Covalency contraction parameter, R_v or R_d , vs $\Delta\chi$ for filled and unfilled d shell cations.

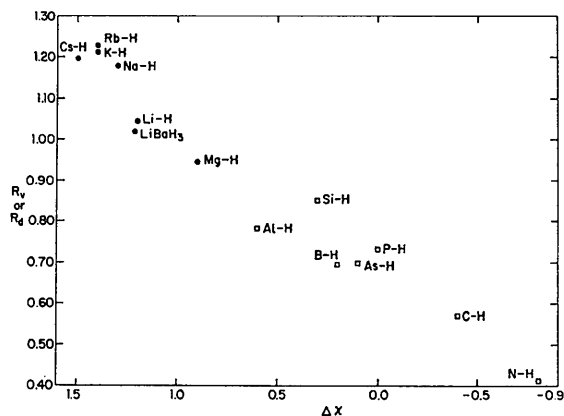


Fig. 8. Covalency contraction parameter, R_v or R_d , vs $\Delta\chi$ for hydrides. Solid circles represent ratios of cell volumes of isotopic compounds. Squares represent ratios of the cubed M-H distances to the cubed M-F distances.

dependence of R_v on $\Delta\chi$. For $\text{Fe}^{2+}\text{-Mg}^{2+}$ the Fe^{2+} fluoride volumes are $\sim 110\%$ of the corresponding Mg^{2+} fluoride volumes whereas the Fe^{2+} sulfide volumes are $\sim 96\%$ of the corresponding Mg^{2+} sulfide volumes. Plots for the cations with filled ' d ' shells show a markedly smaller dependence on $\Delta\chi$. This appears to be due to the difference in covalence of hybrid orbitals formed from metal ' d ' orbitals vs metal ' $s-p$ ' orbitals.

These relations show that effective ionic radii derived primarily from oxides are not strictly applicable to fluorides – note the change in R_v for Fe^{2+} , Co^{2+} , Ni^{2+} , and Mn^{2+} from fluorides to oxides. This effect is particularly noticeable in $R_v\text{-}\Delta\chi$ plots for the pairs $\text{Cu}^+\text{-Li}^+$ and $\text{Ag}^+\text{-Na}^+$ (Shannon & Gummerman, 1975). The $\text{Cu}^+\text{-Li}^+$ and $\text{Ag}^+\text{-Na}^+$ plots are very steep, e.g. the volume of AgF is 120% of the volume of NaF , whereas the volume of Ag_2Se is only 72% of the volume of Na_2Se . Although most of this change arises from covalency, double repulsion effects present in the Li and Na halides described by Pauling (1960) may also play a role.

Covalence effects are useful in explaining certain differences between the effective ionic radii of Table 1 and the ionic radii of Pauling (1927) and Ahrens (1952). Pauling's radii for Cu^+ (0.96 Å) and Ag^+ (1.26 Å) are considerably larger than those in Table 1 (0.77 and 1.15 Å respectively). Since these radii were derived from comparison of alkali halide distances, using an equation relating effective nuclear charge and screening constants (Pauling, 1927), they are valid in primarily ionic crystals. The smaller radii in Table 1 are applicable in the more covalent oxides. Extrapolation of R vs $\Delta\chi$ curves such as in Fig. 7 leads to values of 0.91 Å and 1.23 Å for fluorides, which are close to Pauling's ionic values.

A final example of covalence effects concerns $\text{M}^+\text{-H}^-$ distances. According to Gibb (1962), the radius of the hydride ion is slightly larger than the radius of the fluoride ion. To rationalize the behavior of the hydride ion, the M-H bond has been treated as covalent. Therefore, it is useful to make R_v vs $\Delta\chi$ plots similar to those just discussed for Fe^{2+} , Cu^+ , etc. In this case, the reference ion is F^- and volumes of certain hydrides are compared to those of isotopic fluorides. The results of this analysis are shown in Fig. 8. The solid circles represent volume ratios, $R_v = V(\text{M}_m\text{H}_n)/V(\text{M}_m\text{F}_n)$; open squares represent ratios of typical distances $R_d = d(\text{M-H})^3/d(\text{M-F})^3$. In the more ionic hydrides of Cs, Rb, K, and Na, hydride volumes are considerably larger than those of the fluorides. For the Li and Mg compounds, hydride and fluoride volumes are approximately equal, whereas the more covalent hydrides have increasingly smaller relative volumes than the corresponding fluorides. Fig. 8 partly explains the differences in reported radii. The Morris & Reed (1965) value of 1.53 Å was derived essentially from the large alkali halides, while Gibb's value of 1.40 Å was derived primarily from hydrides of the more electronegative

metals such as: Sc, Ti, Y, Zr, Hf, Nb, Ta, and Th. Because of this strong dependence of M–H distances on cation electronegativity, it does not seem very useful to quote a unique radius for H⁻.

(b) *Tetrahedral oxyanions.* Lack of additivity also appears in most small tetrahedral groups and is particularly noticeable for the ions ^{IV}B³⁺, ^{IV}Fe³⁺, ^{IV}Ge⁴⁺, ^{IV}As⁵⁺, ^{IV}V⁵⁺, ^{IV}S⁶⁺, ^{IV}Se⁶⁺, and ^{IV}Cl⁷⁺. The deviations in vanadates have been studied in detail (Shannon & Calvo, 1973*b*). Assuming that the V–O bond is strongly covalent, and that relatively electronegative cations such as Cu²⁺, Ni²⁺, and Co²⁺ tend to remove electron density from the V–O bond, a V–O bond length increase in Cu, Ni, and Co vanadates is anticipated. Plots of mean radii (\bar{r}) vs mean cation electronegativity ($\bar{\chi}$) show a marked slope with a gradual increase in \bar{r} (^{IV}V⁵⁺) from vanadates of the alkali and alkaline earth ions to those of Cu, Ni, and Co. Similar plots for other ions, P⁵⁺, As⁵⁺ (Shannon & Calvo, 1973*b*), B³⁺, Si⁴⁺, Se⁶⁺ (Shannon, 1975), showed the same behavior. The statistical data on the tetrahedra of B³⁺, Si⁴⁺, Ge⁴⁺, P⁵⁺, As⁵⁺, S⁶⁺, Se⁶⁺, Cr⁶⁺, Mo⁶⁺, W⁶⁺, and Cl⁷⁺ have been summarized by Shannon (1975). The slopes of the \bar{r} vs $\bar{\chi}$ plots were greatest for V⁵⁺, Se⁶⁺, and Cl⁷⁺, and least for Si⁴⁺. Although the evidence for covalence as the origin of these effects in the above systems is only indirect, this behavior is consistent with accepted ideas of ‘covalent shortening’ of bonds.

The evidence for covalent shortening of ^{IV}Fe³⁺–O bonds is more direct. Jeitschko, Sleight, McClellan & Weiher (1976) have found a good correlation between (1) the Fe Mössbauer isomer shift and mean Fe–O distance and (2) $\bar{\chi}$ and mean Fe–O distance (\bar{R}). Thus, in β -NaFeO₂ \bar{R} = 1.86 Å and δ = 0.18 mm s⁻¹ relative to α Fe whereas in Bi₃(FeO₄) (MoO₄)₂ \bar{R} = 1.909 Å and δ = 0.282 mm s⁻¹.

4. Effects of electron delocalization

At a pressure of 6.5 kbar SmS (NaCl structure) undergoes a semiconductor to metal transition and a reduction in cell edge from 5.97 to 5.70 Å (Jayaraman, Narayanamurti, Bucher & Maines, 1970). The reduction in cell volume was attributed to a partial conversion of Sm²⁺ to Sm³⁺; some of the electrons presumably go into a conduction band.

Electron delocalization effects can also be seen by comparing the volumes of the conducting V sulfides VS, V₇S₈, V₃S₄ and V₅S₈ with the corresponding Cr sulfides which have localized ‘*d*’ electrons (de Vries & Jellinek, 1974). The V compounds have volumes ~5% smaller than the corresponding chromium compounds. This does not agree with the relative sizes of V and Cr in oxides and fluorides, e.g. r (^{VI}V³⁺) = 0.64 and r (^{VI}Cr³⁺) = 0.615 Å. For the sulfides, this unit-cell volume anomaly is not simply attributable to metallic vs semiconducting behavior. While Cr₃S₄, Cr₅S₆, and Cr₇S₈ show a positive temperature dependence of resistivity typical of a metal, magnetic susceptibility

measurements indicate Curie–Weiss behavior and therefore nearly localized electrons (van Bruggen, 1969). This is in contrast to the Pauli paramagnetic behavior of the corresponding V sulfides (de Vries & Haas, 1973) characteristic of delocalized electrons. Thus, in SmS and the sulfides of V metallic character accompanied by electron delocalization appears to be associated with reduced bond distances.

A further example of delocalization effects occurs in the compound NaVS₂ (Weigers, van der Meer, van Heinigen, Kloosterboer & Alberink, 1974). The molecular volume of Pauli paramagnetic NaVS₂ I (67.9 Å³) is significantly less than that of NaVS₂ II (72.7 Å³). NaVS₂ II is characterized by localized electrons (Jellinek, 1975) and its molecular volume is consistent with that of isotopic NaCrS₂ (71.1 Å³).

If electron delocalization in oxides results in reduced metal–oxygen distances and thereby an effective increase in valence, radii derived for the ions Mo⁴⁺, Tc⁴⁺, Ru⁴⁺, Rh⁴⁺, W⁴⁺, Re⁴⁺, Os⁴⁺, and Ir⁵⁺ from metallic oxides may not be reliable when applied to insulating oxides. Thus, radii obtained from distances in the metallic phases, e.g. RhO₂, ReO₂, and Cd₂Ir₂O₇, will be smaller than radii obtained from semiconducting or insulating compounds.* When both types of compounds have been studied, a significant difference in distances is generally found. The mean octahedral Re⁴⁺–O distance in insulating K₄[Re₂O₂(C₂O₄)₄].3H₂O (Lis, 1975) of 2.021 (10) Å (r = 0.671 Å) is greater than the estimated mean distance in metallic ReO₂ of 1.99 Å (r = 0.63 Å). Knop & Carlow’s (1974) value of r = 0.662 Å derived from cell volumes of the insulating Cs₂ReF₆ phases is consistent with the radius of Re⁴⁺ from K₄[Re₂O₂(C₂O₄)₄].3H₂O. The Re⁵⁺–O distance in Nd₄Re₂O₁₁ (Wilhelmi, Lagervall & Muller, 1970) of 1.987 (12) Å (r = 0.607 Å) is significantly greater than the distance in metallic Cd₂Re₂O₇ (Sleight, 1975) of 1.93 (2) Å (r = 0.55 Å). The radii of 0.58 Å derived from XeF₂RuF₆ and 0.60 Å from XeFRuF₆ (Bartlett, Gennis, Gibler, Morrell & Zalkin, 1973) are greater than the radius of 0.565 Å derived from the r^3 – V plot for metallic Cd₂Ru₂O₇. In contrast, however, the Mo⁴⁺ radius of 0.64 Å derived from insulating Li₂MoF₆ (Brunton, 1971) is not greatly different from the radius of 0.65 Å derived from metallic MoO₂ (Brandt & Skapski, 1967).

Although there appears to be ample evidence to show that M–O bond distances in compounds with localized electrons are greater than M–O distances in compounds with delocalized electrons, the data are not yet sufficient to derive a reliable set of radii for semiconducting compounds containing Mo⁴⁺, Tc⁴⁺, Ru⁴⁺, Rh⁴⁺, W⁴⁺, Re⁴⁺, Os⁴⁺, and Ir⁵⁺. This will become possible as additional accurate structure refinements of fluorides, molecular inorganic compounds, and semiconducting oxides containing these ions become available.

* This assumes that metallic character can be equated with delocalized electron behavior in these compounds.

I would like to acknowledge the help of F. Jelinek for providing unpublished data on NaVS_2 , F. C. Hawthorne for pointing out numerous structures containing partially occupied cation sites, O. Muller for several sources of radii of unusual ions, M. Fouassier for unpublished data on K_4MO_4 compounds, I. D. Brown for unpublished bond length-bond strength curves, and P. S. Gumerman for assistance with data collection. Structure data on rare earth halides and an analysis of the radii of divalent rare earths provided by H. Bärnighausen were especially valuable. I am particularly indebted to Ruth Shannon for the tabulation of data and proof reading. Finally, I would like to thank R. J. Bouchard, W. H. Baur, and H. Bärnighausen for critically reviewing the manuscript prior to publication.

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